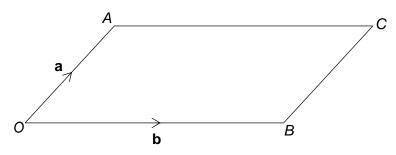


## **Vectors**



## REVISE THIS **TOPIC**

1 OACB is a parallelogram.



$$\overrightarrow{OA} = \mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

Write the following vectors in terms of **a** and **b**.

 $\overrightarrow{AO}$ [1 mark] 1 (a)

> a Answer\_

 $\overrightarrow{BC}$ 1 (b) [1 mark]

Answer

 $\overrightarrow{AB}$ [1 mark] 1 (c)

Answer\_

 $\overrightarrow{co}$ 1 (d) [1 mark]

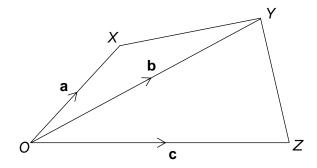
Answer







2 OXYZ is a quadrilateral.



$$\overrightarrow{OX} = \mathbf{a}$$

$$\overrightarrow{OY} = \mathbf{b}$$

$$\overrightarrow{OZ} = \mathbf{c}$$

Write the following vectors in terms of **a**, **b** and **c**.

2 (a)  $\overrightarrow{ZO}$ 

[1 mark]

Answer

2 (b)  $\overrightarrow{XY}$ 

[1 mark]

b-a

2 (c)  $\overrightarrow{ZY}$ 

[1 mark]

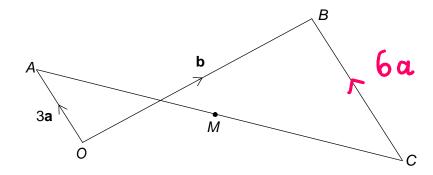
Answer \_\_\_\_\_\_ b - C

2 (d)  $\overrightarrow{XZ}$ 

[1 mark]

Answer





$$\overrightarrow{OA} = 3\mathbf{a}$$

$$\overrightarrow{OB} = \mathbf{b}$$

$$\overrightarrow{CB} = 2\overrightarrow{OA}$$

Write the following vectors in terms of **a**, **b** and **c**.

3 (a) 
$$\overrightarrow{AB}$$

[1 mark]

3 (b)

$$\overrightarrow{CA} = \overrightarrow{CB} + \overrightarrow{BO} + \overrightarrow{OA}$$

[2 marks]

Answer 
$$q_{a-b}$$

3 (c) *M* is the midpoint of AC.

Write  $\overrightarrow{CM}$  in terms of **a** and **b**.

[2 marks]

$$CM$$
 in terms of  $a$  and  $b$ .

 $CM = \frac{1}{2}CA$ 
 $= \frac{1}{2}(9a - b)$ 

Answer

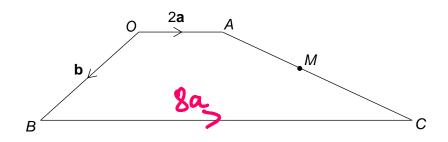
9 a - 12 b



Turn over ▶

9

OACB is a trapezium



$$\overrightarrow{OA} = 2\mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$   $\overrightarrow{BC} = 4\overrightarrow{OA}$ 

Write  $\overrightarrow{AC}$  in term of **a** and **b**. 4 (a)

e 
$$AC$$
 in term of a and b. [2 marks]
$$AC = AO + OB + BC$$

$$= -2a + b + 8a$$

Answer 
$$6a+b$$

4 (b) *M* is the midpoint of *AC*.

Write 
$$\overrightarrow{BM}$$
 in term of a and b.

$$\overrightarrow{BM} = \overrightarrow{BO} + \overrightarrow{OA} + \cancel{AC}$$

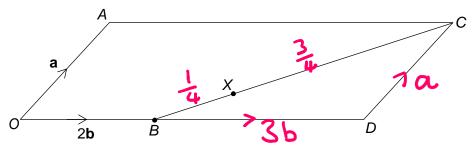
$$= -b + 2a + \cancel{A}(6a + b)$$

$$= -b + 2a + 3a + \cancel{Ab}$$





5 OACD is a parallelogram.



$$\overrightarrow{OA} = \mathbf{a}$$
  $\overrightarrow{OB} = 2\mathbf{b}$   $\overrightarrow{OD} = 2.5 \overrightarrow{OB}$ 

Write  $\overrightarrow{AD}$  in term of **a** and **b**. 5 (a)

$$\overrightarrow{AD} = \overrightarrow{A0} + \overrightarrow{OD}$$

$$= -\alpha + 5b$$

Answer 
$$5b - a$$

Write  $\overrightarrow{BC}$  in term of **a** and **b**. 5 (b)

$$\overrightarrow{BC} = \overrightarrow{BD} + \overrightarrow{DC}$$
 [2 marks]

$$= 3b + a$$

Answer 
$$3b + a$$

5 (c) BX: XC = 1:3

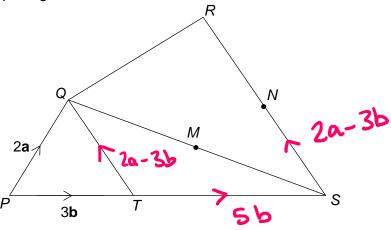
Write  $O\hat{X}$  in term of **a** and **b**.

[2 marks]

$$\overrightarrow{OX} = \overrightarrow{OB} + \overrightarrow{BX}$$

Answer

6 PQRST is a pentagon.



$$\overrightarrow{PQ} = 2\mathbf{a}$$

$$\overrightarrow{PT} = 3\mathbf{b}$$

$$\overrightarrow{RS} = 2\overrightarrow{QT}$$

PTS is a straight line with PT: TS = 3:5

*M* is the midpoint of *QS*. *N* is the midpoint of *RS*.

1 TS=56

Write  $\stackrel{\longrightarrow}{MN}$  in term of **a** and **b**.

[4 marks]

$$QS = QT + TS$$

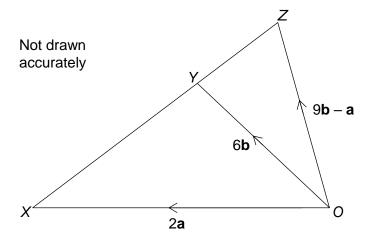
$$= 3b - 2a + 5b$$

$$= 8b - 2a$$

$$= 4b - a + 2a - 3b$$

Answer Q + b





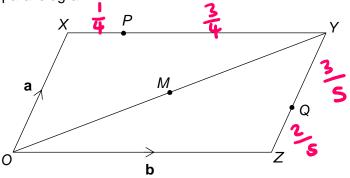
Prove, using vectors, that XYZ is a straight line.

[3 marks]



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OXYZ is a parallelogram



$$\overrightarrow{OX} = \mathbf{a}$$

$$\overrightarrow{OZ} = \mathbf{b}$$

$$XP: PY = 1:3$$
  
 $ZQ: QY = 2:3$ 

*M* is the midpoint of *OY* 

8 (a)

Write  $\overrightarrow{PQ}$  in term of **a** and **b**.

[2 marks]

Answer\_

4b - 30

8 (b)

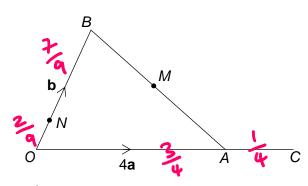
Write  $\overrightarrow{MQ}$  in term of **a** and **b**.

[3 marks]

$$= \frac{1}{2}(a+b) - \frac{3}{5}a$$

Answer





$$\overrightarrow{OA} = 4\mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

OA: OC = 3:4ON: OB = 2:9

M is the midpoint of AB

9 (a) Write  $\overrightarrow{MC}$  in term of a and b.

[3 marks]

Answer 
$$\frac{10}{3}a - \frac{1}{2}b$$

9 (b) Write  $\overrightarrow{NM}$  in term of **a** and **b**.

[2 marks]

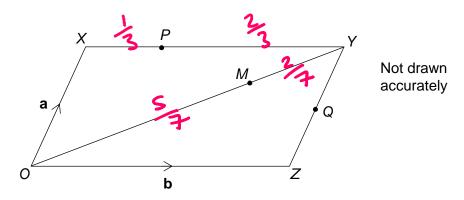
Answer  $\frac{3}{18}b + 2a$ 

10





10 OXYZ is a parallelogram



$$\overrightarrow{OX} = \mathbf{a}$$
  $\overrightarrow{OZ} = \mathbf{b}$ 

ZQ = QY XP: PY = 1:2 OM: MY = 5:2

Prove, using vectors, that PMQ is a straight line.

[4 marks]

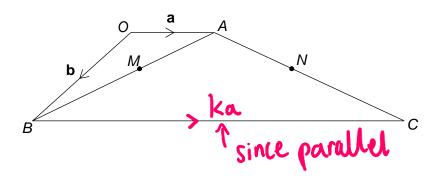
$$PM = PY + YM$$
=  $PY + YM$ 
=  $PX + PM$ 

Therefore  $PMQ$  is a straight line





11 OACB is a trapezium



$$\overrightarrow{OA} = \mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

M and N are the midpoints of AB and AC.

Prove, using vectors, that MN is parallel to OA.

[4 marks]

$$MN = MA + AN$$

$$= 2BA + 2AC$$

$$= 2(a-b) + 2(-a+b+ka)$$

$$= 2a - 2b - 2a + 2b + 2a$$

$$= 2a$$

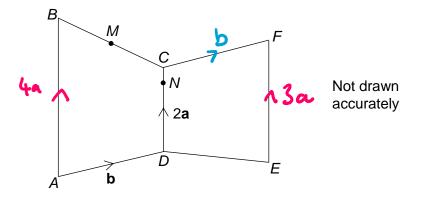
therefore they are parallel



3 |



## 12 ABCD and CDEF are trapeziums



$$\overrightarrow{DC} = 2\mathbf{a}$$
  $\overrightarrow{AD} = \overrightarrow{CF} = \mathbf{b}$ 

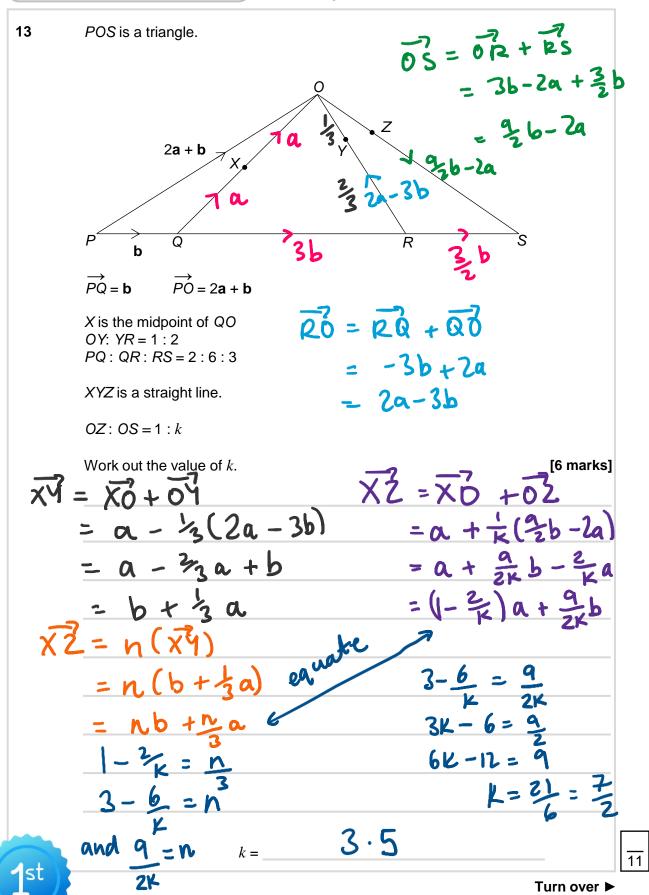
AB:DC:EF=4:2:3 M is the midpoint of BC. N is on the line CD.

MNE is a straight line.

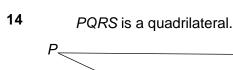
DN : NC = k : 1, where k is an integer.

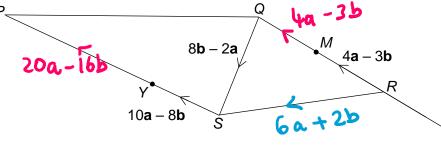
MN =  $\frac{MC + CN}{MC + CN}$   $= \frac{MC + CN}{NE} = \frac{NC + CF}{NC} + \frac{FE}{NC}$   $= \frac{1}{2}(BC) + CN$   $= \frac{1}{2}(AC) + CN$   $= \frac{1}{2}$ 











$$\overrightarrow{SY} = 10\mathbf{a} - 8\mathbf{b}$$

$$\overrightarrow{QS} = 8\mathbf{b} - 2\mathbf{a}$$

$$\overrightarrow{RM} = 4\mathbf{a} - 3\mathbf{b}$$

RM = MQ

SY: YP = 1:2

QRX is a straight line.

XS is parallel to RP.

Work out XS: RP

Give your answer in the form n:1

[6 marks]

$$\vec{R}\vec{P} = \vec{R}\vec{Q} + \vec{Q}\vec{S} + \vec{S}\vec{P}$$

$$= K(4a-3b) + 6a + 2b$$

$$= (4K + 6)a - (3K - 2)b$$

$$4K + 6 = 36n (x3)$$

$$3K - 2 = 22n (x4)$$

$$n = 26$$

$$n = 13$$

10

Answer

1.3:1

