

## Circle Theorems



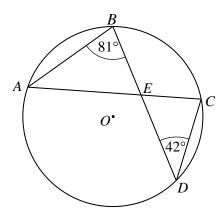


## REVISE THIS **TOPIC**

CHECK YOUR ANSWERS



A, B, C and D are points on the circumference of a circle with centre O.



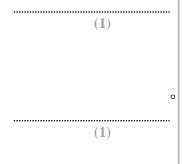
Angle  $ABD = 81^{\circ}$ Angle  $BDC = 42^{\circ}$ 

(a) Work out the size of angle CAB.

(b) Work out the size of angle ACD.

(c) Work out the size of angle AEB.

(d) Work out the size of angle BEC.



(1)

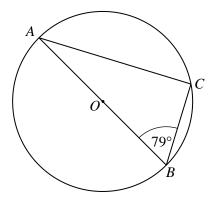
(Total for Question 1 is 4 marks)











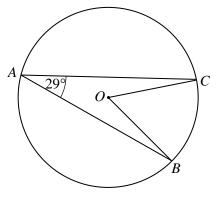
Angle  $ABC = 79^{\circ}$ 

(a) Work out the size of angle CAB.

(b) Give a reason for your answer to part (a)

(Total for Question 2 is 2 marks)

A, B and C are points on the circumference of a circle with centre O.



Angle  $CAB = 29^{\circ}$ 

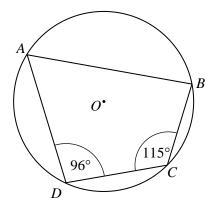
(a) Work out the size of angle *COB*.

(b) Give a reason for your answer to part (a)



(Total for Question 3 is 2 marks)

Solutions



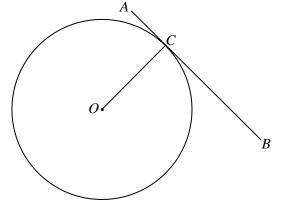
Angle  $ADC = 96^{\circ}$ Angle  $BCD = 115^{\circ}$ 

(a) Work out the size of angle ABC.

(b) Give a reason for your answer to part (a)

(Total for Question 4 is 2 marks)

A, B, and C are points on the circumference of a circle with centre O. AB is the tangent to the circle at point C.



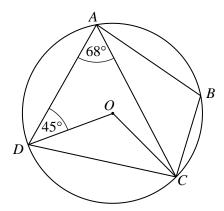
(a) Write down the size of angle *OCB*.

(b) Give a reason for your answer to part (a)



(Total for Question 5 is 2 marks)

Solutions



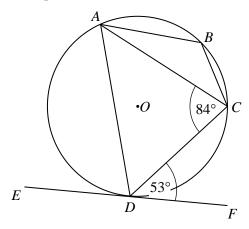
Angle  $DAC = 68^{\circ}$ Angle  $ADO = 45^{\circ}$ 

Work out the size of angle *ABC*. Give reasons for each stage of your working.

(Total for Question 6 is 4 marks)



7 A, B, C and D are points on the circumference of a circle with centre O. EF is the tangent to the circle at point D.



Angle  $ACD = 84^{\circ}$ 

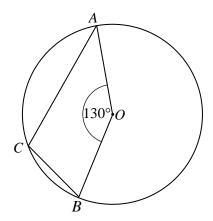
Angle  $CDF = 53^{\circ}$ 

Work out the size of angle *ABC*.

Give reasons for each stage of your working.

(Total for Question 7 is 4 marks)



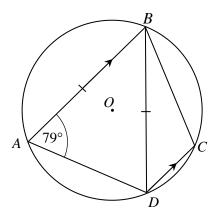


Angle  $AOB = 130^{\circ}$ 

Work out the size of angle *ACB*. Give reasons for each stage of your working.

(Total for Question 8 is 3 marks)





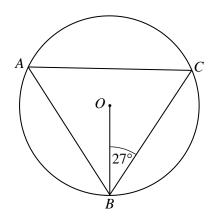
Angle  $BAD = 79^{\circ}$  BA = BDLines AB and DC are parallel.

Work out the size of angle *DBC*. Give reasons for each stage of your working.

1st

Solutions



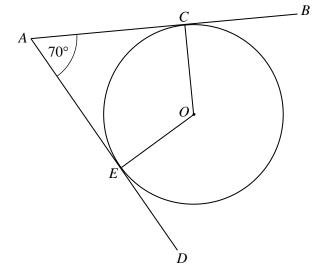


Angle  $CBO = 27^{\circ}$ 

Work out the size of angle *BAC*. Give reasons for each stage of your working.

(Total for Question 10 is 3 marks)





AB and AD are tangents to the circle at C and E. Angle  $EAC = 70^{\circ}$ 

(a) Work out the size of angle COE.

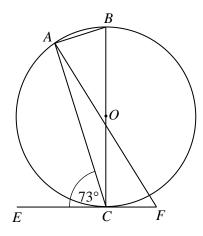
OC = 5 cm

(2)

(b) Work out the length of *CA*. Give your answer to 1 decimal place.

......cm

(Total for Question 11 is 4 marks)



EF is the tangent to the circle at C.

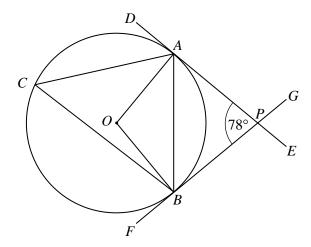
Angle  $ACE = 73^{\circ}$ 

Angle  $FAB = 5 \times Angle CAF$ 

Work out the size of angle AFC.

(Total for Question 12 is 4 marks)





*DE* and *FG* are tangents to the circle at *A* and *B* that intersect at the point *P*. Angle  $APB = 78^{\circ}$ 

(a) Work out the size of angle ACB.

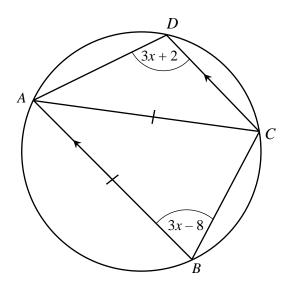
(b) Work out the size of angle ABP.

(2)



(Total for Question 13 is 4 marks)

14



A, B, C and D are points on the circumference of a circle. ABCD is a trapezium with AB parallel to DC.

AB = AC

Work out the size of angle DAC.

You must show all your working.

(Total for Question 14 is 5 marks)

 $\begin{array}{c}
C \\
B \\
\hline
O \\
5x-7
\end{array}$ 

B and D are points on the circumference of a circle, centre O. ABC and ADE are tangents to the circle.

(a) Work out value of *x*. You must show all your working.

x = (3)

AD = 30 cm

(b) Work out the radius of the circle. Give your answer to three significant figures.

..... cm

(Total for Question 15 is 6 marks)