



Completing the Square



←
REVISE THIS TOPIC

1 Write $x^2 + 6x + 11$ in the form $(x + a)^2 + b$

$$(x + 3)^2 - 9 + 11$$

$$(x + 3)^2 + 2$$

(Total for Question 1 is 2 marks)

2 Write $x^2 + 8x + 30$ in the form $(x + a)^2 + b$

$$(x + 4)^2 - 16 + 30$$

$$(x + 4)^2 + 14$$

(Total for Question 2 is 2 marks)

3 Write $x^2 + 4x + 1$ in the form $(x + a)^2 - b$

$$(x + 2)^2 - 4 + 1$$

$$(x + 2)^2 - 3$$

(Total for Question 3 is 2 marks)



4 Write $x^2 - 10x + 12$ in the form $(x - a)^2 - b$

$$(x - 5)^2 - 25 + 12$$

$$(x - 5)^2 - 13$$

(Total for Question 4 is 2 marks)

5 Write $x^2 - 2x + 13$ in the form $(x - a)^2 + b$

$$(x - 1)^2 - 1 + 13$$

$$(x - 1)^2 + 12$$

(Total for Question 5 is 2 marks)

6 Write $x^2 - 12x - 16$ in the form $(x - a)^2 + b$

$$(x - 6)^2 - 36 - 16$$

$$(x - 6)^2 - 52$$

(Total for Question 6 is 2 marks)

7 Write $x^2 - 20x$ in the form $(x - a)^2 - b$

$$(x - 10)^2 - 100$$

$$(x - 10)^2 - 100$$

(Total for Question 7 is 2 marks)



8 Write $x^2 + 3x + 5$ in the form $(x + a)^2 + b$

$$\begin{aligned} & \left(x + \frac{3}{2}\right)^2 - \frac{9}{4} + 5 \\ & \left(x + \frac{3}{2}\right)^2 - \frac{9}{4} + \frac{20}{4} \end{aligned}$$

$$\left(x + \frac{3}{2}\right)^2 + \frac{11}{4}$$

(Total for Question 8 is 3 marks)

9 Write $x^2 - 5x + 7$ in the form $(x - a)^2 + b$

$$\begin{aligned} & \left(x - \frac{5}{2}\right)^2 - \frac{25}{4} + 7 \\ & \left(x - \frac{5}{2}\right)^2 - \frac{25}{4} + \frac{28}{4} \end{aligned}$$

$$\left(x - \frac{5}{2}\right)^2 + \frac{3}{4}$$

(Total for Question 9 is 3 marks)

10 Write $x^2 + 9x + 3$ in the form $(x + a)^2 - b$

$$\begin{aligned} & \left(x + \frac{9}{2}\right)^2 - \frac{81}{4} + 3 \\ & \left(x + \frac{9}{2}\right)^2 - \frac{81}{4} + \frac{12}{4} \end{aligned}$$

$$\left(x + \frac{9}{2}\right)^2 - \frac{69}{4}$$

(Total for Question 10 is 3 marks)

11 Write $x^2 - x - 2.75$ in the form $(x - a)^2 - b$

$$\left(x - \frac{1}{2}\right)^2 - \frac{1}{4} - 2\frac{3}{4}$$

$$\left(x - \frac{1}{2}\right)^2 - 3$$

(Total for Question 11 is 3 marks)



12 Here is an identity

$$x^2 + px + 32 \equiv (x + 5)^2 - q$$

Work out the values of p and q .

$$x^2 + \underbrace{px}_{10x} + 32 \equiv x^2 + \underbrace{10x}_{10x} + \underbrace{25 - q}_{-7}$$

$$px = 10x$$

$$p = 10$$

$$32 = 25 - q$$

$$q = 25 - 32$$

$$q = -7$$

$$p = \underline{\quad 10 \quad}$$

$$q = \underline{\quad -7 \quad}$$

(Total for Question 12 is 3 marks)

13 Here is an identity

$$x^2 - 8x + p \equiv (x + q)^2 - 4$$

Work out the values of p and q .

$$x^2 - \underbrace{8x}_{2qx} + \underbrace{p}_{q^2 - 4} \equiv x^2 + \underbrace{2qx}_{2qx} + \underbrace{q^2 - 4}_{q^2 - 4}$$

$$-8x = 2qx$$

$$-8 = 2q$$

$$q = -4$$

$$p = q^2 - 4$$

$$p = (-4)^2 - 4$$

$$p = 16 - 4$$

$$p = \underline{\quad 12 \quad}$$

$$q = \underline{\quad -4 \quad}$$

(Total for Question 12 is 3 marks)

