

# **Vectors**

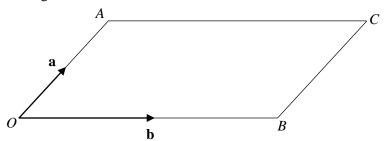




CHECK YOUR ANSWERS



OACB is a parallelogram. 1



$$\overrightarrow{OA} = \mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

Work out the following vectors in terms of  $\mathbf{a}$  and  $\mathbf{b}$ .

$$(a)_{AO}$$

 $(b)\overrightarrow{BC}$ 

 $(c)_{\overrightarrow{AB}}$ 

 $(d)_{CO}$ 

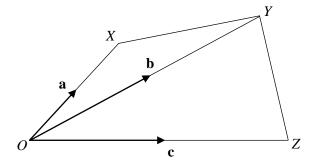
(1)

(Total for Question 1 is 4 marks)





## 2 OXYZ is a quadrilateral.



$$\overrightarrow{OX} = \mathbf{a}$$
  $\overrightarrow{OY} = \mathbf{b}$   $\overrightarrow{OZ} = \mathbf{c}$ 

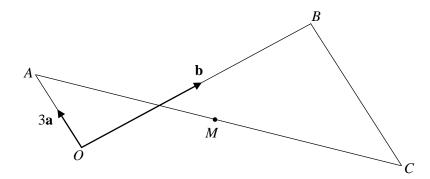
Work out the following vectors in terms of **a** and **b**.

- (a)  $\overrightarrow{ZO}$
- (b)  $\overrightarrow{XY}$
- (c)  $\overrightarrow{ZY}$
- (d)  $\overrightarrow{XZ}$

(1)

(Total for Question 2 is 4 marks)

3



$$\overrightarrow{OA} = 3\mathbf{a}$$

$$\xrightarrow{OR-1}$$

$$\overrightarrow{CB} = 2\overrightarrow{OA}$$

Write the following vectors in terms of **a**, **b** and **c**.

Work out the following vectors in terms of **a** and **b**.

(a)  $\overrightarrow{AB}$ 

(b)  $\overrightarrow{CA}$ 

(2)

(1)

M is the midpoint of AC.

(c) Write  $\overrightarrow{CM}$  in terms of **a** and **b**.



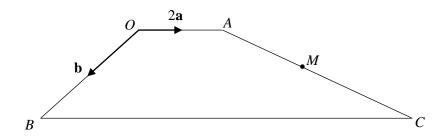
(Total for Question 3 is 5 marks)

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### 4 *OACB* is a trapezium



$$\overrightarrow{OA} = 2\mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$   $\overrightarrow{BC} = 4\overrightarrow{C}$ 

(a) Write  $\overrightarrow{AC}$  in terms of **a** and **b**.

(2)

M is the midpoint of AC.

(b) Write  $\overrightarrow{BM}$  in terms of **a** and **b**.

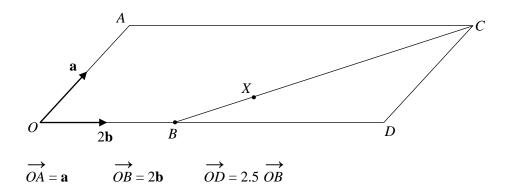
(3)

(Total for Question 4 is 5 marks)





5 *OACD* is a parallelogram.



(a) Write  $\overrightarrow{AD}$  in terms of **a** and **b**.

(b) Write  $\overrightarrow{BC}$  in terms of **a** and **b**.

(2)

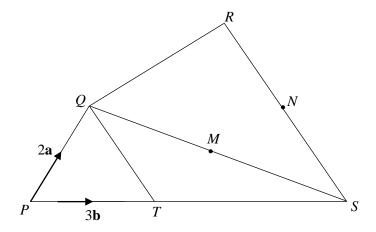
BX : XC = 1 : 3

(c) Write  $\overrightarrow{OX}$  in terms of **a** and **b**.

(2)

(Total for Question 5 is 6 marks)

#### PQRS is a quadrilateral



$$\overrightarrow{PQ} = 2\mathbf{a}$$

$$\overrightarrow{PT} = 3\mathbf{h}$$

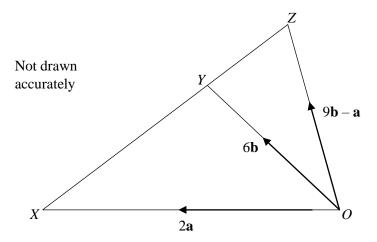
$$\overrightarrow{RS} = 2\overrightarrow{QT}$$

*PTS* is a straight line with PT: TS = 3:5

M is the midpoint of QS. *N* is the midpoint of *RS*.

Write  $\overrightarrow{MN}$  in term of **a** and **b**.

7



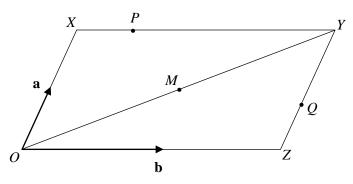
Prove, using vectors, that XYZ is a straight line.



Solutions



OXYZ is a parallelogram



$$\overrightarrow{OX} = \mathbf{a}$$
  $\overrightarrow{OZ} = \mathbf{b}$ 

$$XP : PY = 1 : 3$$
  
 $ZQ : QY = 2 : 3$ 

M is the midpoint of OY

(a) Write  $\overrightarrow{PQ}$  in terms of **a** and **b**.

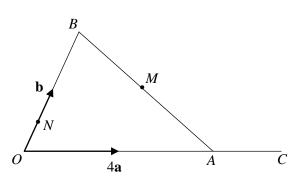
(b) Write  $\overrightarrow{MQ}$  in terms of **a** and **b**.

(2)



(Total for Question 8 is 5 marks)

9



$$\overrightarrow{OA} = 4\mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

$$OA : OC = 3 : 4$$
  
 $ON : OB = 2 : 9$ 

M is the midpoint of AB

(a) Write  $\overrightarrow{MC}$  in terms of **a** and **b**.

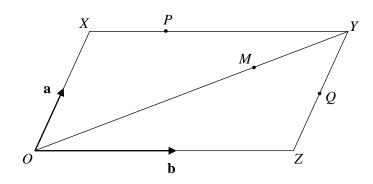
(b) Write  $\overrightarrow{NM}$  in terms of **a** and **b**.



(Total for Question 9 is 5 marks)



#### **10** *OXYZ* is a parallelogram



$$\overrightarrow{OX} = \mathbf{a}$$
  $\overrightarrow{OZ} = \mathbf{b}$ 

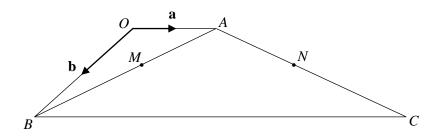
$$ZQ = QY$$
$$XP: PY = 1:2$$

XP : PY = 1 : 2OM : MY = 5 : 2

Prove, using vectors, that PMQ is a straight line.



#### 11 OACB is a trapezium



$$\overrightarrow{OA} = \mathbf{a}$$
  $\overrightarrow{OB} = \mathbf{b}$ 

M and N are the midpoints of AB and AC.

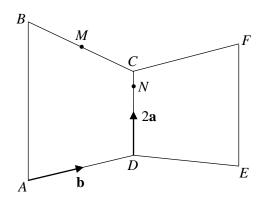
Prove, using vectors, that MN is parallel to OA.



Solutions



#### **12** ABCD and CDEF are trapeziums



$$\overrightarrow{DC} = 2\mathbf{a}$$
  $\overrightarrow{AD} = \overrightarrow{CF} = \mathbf{b}$ 

AB : DC : EF = 4 : 2 : 3 M is the midpoint of BC. N is on the line CD.

MNE is a straight line.

DN : NC = k : 1, where k is an integer.

Work out the value of k.

<i>k</i> =	:
к –	· ······

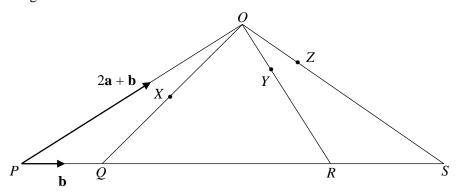
(Total for Question 12 is 5 marks)





12

#### **13** *POS* is a triangle.



$$\overrightarrow{PQ} = \mathbf{b}$$

$$\overrightarrow{PO} = 2\mathbf{a} + \mathbf{b}$$

X is the midpoint of QO

*OY*: YR = 1:2

PQ: QR: RS = 2:6:3

XYZ is a straight line.

OZ:OS=1:k

Work out the value of k.

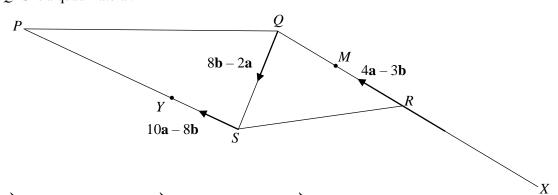
1st

*k* = .....

(Total for Question 13 is 6 marks)



## **14** *PQRS* is a quadrilateral.



$$\overrightarrow{SY} = 10\mathbf{a} - 8\mathbf{b}$$

$$Q\hat{S} = 8\mathbf{b} - 2\mathbf{a}$$

$$\overrightarrow{QS} = 8\mathbf{b} - 2\mathbf{a}$$
  $\overrightarrow{RM} = 4\mathbf{a} - 3\mathbf{b}$ 

$$RM = MQ$$

$$SY : YP = 1 : 2$$

QRX is a straight line.

XS is parallel to RP.

Work out XS: RP

Give your answer in the form n:1



(Total for Question 14 is 6 marks)