## Vectors

$1 \quad O A C B$ is a parallelogram.

$\overrightarrow{O A}=\mathbf{a} \quad \overrightarrow{O B}=\mathbf{b}$
Work out the following vectors in terms of $\mathbf{a}$ and $\mathbf{b}$.
(a) $\overrightarrow{A O}$
(b) $\overrightarrow{B C}$
(c) $\overrightarrow{A B}$
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$2 O X Y Z$ is a quadrilateral.

$\overrightarrow{O X}=\mathbf{a} \quad \overrightarrow{O Y}=\mathbf{b} \quad \overrightarrow{O Z}=\mathbf{c}$

Work out the following vectors in terms of $\mathbf{a}$ and $\mathbf{b}$.
(a) $\overrightarrow{\mathrm{ZO}}$
(b) $\overrightarrow{X Y}$
(c) $\overrightarrow{Z Y}$
(d) $\overrightarrow{X Z}$

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Write the following vectors in terms of $\mathbf{a}, \mathbf{b}$ and $\mathbf{c}$.

Work out the following vectors in terms of $\mathbf{a}$ and $\mathbf{b}$.
(a) $\overrightarrow{A B}$
(b) $\overrightarrow{C A}$
$M$ is the midpoint of $A C$.
(c) Write $\overrightarrow{C M}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.

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$4 O A C B$ is a trapezium

(a) Write $\overrightarrow{A C}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
$M$ is the midpoint of $A C$.
(b) Write $\overrightarrow{B M}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
$5 O A C D$ is a parallelogram.


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\overrightarrow{O A}=\mathbf{a} \quad \overrightarrow{O B}=2 \mathbf{b} \quad \overrightarrow{O D}=2.5 \overrightarrow{O B}
$$

(a) Write $\overrightarrow{A D}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
(b) Write $\overrightarrow{B C}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
$B X: X C=1: 3$
(c) Write $\overrightarrow{O X}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
$6 P Q R S$ is a quadrilateral


$$
\overrightarrow{P Q}=2 \mathbf{a} \quad \overrightarrow{P T}=3 \mathbf{b} \quad \overrightarrow{R S}=2 \overrightarrow{Q T}
$$

$P T S$ is a straight line with $P T: T S=3: 5$
$M$ is the midpoint of $Q S$.
$N$ is the midpoint of $R S$.
Write $\overrightarrow{M N}$ in term of $\mathbf{a}$ and $\mathbf{b}$.

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Prove, using vectors, that $X Y Z$ is a straight line.
$8 O X Y Z$ is a parallelogram

$\overrightarrow{O X}=\mathbf{a} \quad \overrightarrow{O Z}=\mathbf{b}$
$X P: P Y=1: 3$
$Z Q: Q Y=2: 3$
$M$ is the midpoint of $O Y$
(a) Write $\overrightarrow{P Q}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
(b) Write $\overrightarrow{M Q}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.

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$\overrightarrow{O A}=\mathrm{a} \quad \overrightarrow{\mathrm{a}} \quad \overrightarrow{\mathrm{O}}=\mathrm{b}$
OA: OC $=3: 4$
$O N: O B=2: 9$
$M$ is the midpoint of $A B$
(a) Write $\overrightarrow{M C}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
(b) Write $\overrightarrow{N M}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
$10 O X Y Z$ is a parallelogram

$\overrightarrow{O X}=\mathbf{a} \quad \overrightarrow{O Z}=\mathbf{b}$
$Z Q=Q Y$
$X P: P Y=1: 2$
$O M: M Y=5: 2$
Prove, using vectors, that $P M Q$ is a straight line.

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$11 O A C B$ is a trapezium

$\overrightarrow{O A}=\mathbf{a} \quad \overrightarrow{O B}=\mathbf{b}$
$M$ and $N$ are the midpoints of $A B$ and $A C$.
Prove, using vectors, that $M N$ is parallel to $O A$.
$12 A B C D$ and $C D E F$ are trapeziums

$\overrightarrow{D C}=2 \mathbf{a} \quad \overrightarrow{A D}=\overrightarrow{C F}=\mathbf{b}$
$A B: D C: E F=4: 2: 3$
$M$ is the midpoint of $B C$.
$N$ is on the line $C D$.
$M N E$ is a straight line.
$D N: N C=k: 1$, where $k$ is an integer.
Work out the value of $k$.

$$
k=
$$

$13 P O S$ is a triangle.

$\overrightarrow{P Q}=\mathbf{b} \quad \overrightarrow{P O}=2 \mathbf{a}+\mathbf{b}$
$X$ is the midpoint of $Q O$
$O Y: Y R=1: 2$
$P Q: Q R: R S=2: 6: 3$
$X Y Z$ is a straight line.
$O Z: O S=1: k$

Work out the value of $k$.
$\qquad$
$14 P Q R S$ is a quadrilateral.

$\overrightarrow{S Y}=10 \mathbf{a}-8 \mathbf{b}$
$\overrightarrow{Q S}=8 \mathbf{b}-2 \mathbf{a}$
$\overrightarrow{R M}=4 \mathbf{a}-3 \mathbf{b}$
$R M=M Q$
$S Y: Y P=1: 2$
$Q R X$ is a straight line.
$X S$ is parallel to $R P$.
Work out $X S: R P$
Give your answer in the form $n: 1$

