## Algebraic Fractions (Operations)

## REVISE THIS

 TOPIC1 Write $\frac{5 y}{6}+\frac{y}{4}$ as a single fraction in its simplest form.

$$
\frac{10 y}{12}+\frac{3 y}{12}
$$



2 Write $\frac{x}{2}-\frac{2 x}{5}$ as a single fraction in its simplest form.

$$
\frac{5 x}{10}-\frac{4 x}{10}
$$



3 Write $\frac{1}{3 a}+\frac{4}{a}$ as a single fraction in its simplest form.
[2 marks]

$$
\frac{1}{3 a}+\frac{12}{3 a}
$$

$4 \quad$ Write $\frac{4 b}{5} \times \frac{b}{6}$ as a single fraction in its simplest form.
$\frac{4 b^{2}}{30}$

$$
\text { Answer } \quad \frac{2 b^{2}}{15}
$$

$5 \quad$ Write $\frac{4 c}{9} \div \frac{8}{3 c^{2}}$ as a single fraction in its simplest form.

$$
\frac{4 c}{9} \times \frac{3 c^{2}}{8}=\frac{12 c^{3}}{72}
$$


$6 \quad$ Write $\frac{3 x y}{4} \times \frac{y}{6 x}$ as a single fraction in its simplest form.
$\frac{3 x y^{2}}{24 x}$
$\qquad$

$7 \quad$ Write $\frac{4}{a}+\frac{3}{b}-\frac{7}{a b}$ as a single fraction in its simplest form.

$$
\frac{4 b}{a b}+\frac{3 a}{a b}-\frac{7}{a b}
$$

$$
\text { Answer } \quad \frac{4 b+3 a-7}{a b}
$$

$8 \quad$ Write $\frac{2 x}{y} \times \frac{5}{3 x^{2}} \times \frac{y^{6}}{20}$ as a single fraction in its simplest form.

$$
\frac{10 x y^{6}}{60 x^{2} y}
$$



9 Write $\frac{2}{x y}+\frac{y}{x}+\frac{6}{x^{2}}$ as a single fraction in its simplest form.

$$
\frac{2 x}{x^{2} y}+\frac{x y^{2}}{x^{2} y}+\frac{6 y}{x^{2} y}
$$

$$
\text { Answer } \frac{2 x+x y^{2}+6 y}{x^{2} y}
$$

10 Write $\frac{5}{2 x^{2} y}-\frac{3}{8 x y^{3}}$ as a single fraction in its simplest form.

$$
\frac{20 y^{2}}{8 x^{2} y^{3}}-\frac{3 x}{8 x^{2} y^{3}}
$$

$$
\text { Answer } \quad \frac{20 y^{2}-3 x}{8 x^{2} y^{3}}
$$

11 Write $\frac{10 x y}{6 m^{2} n^{2}} \div \frac{5 x^{2} y^{2}}{9 m n^{5}}$ as a single fraction in its simplest form.

$$
\frac{10 x y}{6 m^{2} n^{2}} \times \frac{9 m n^{5}}{5 x^{2} y^{2}}=\frac{90 m n^{5} x y}{30 m^{2} n^{2} x^{2} y^{2}}
$$

$$
\text { Answer } \quad \frac{3 n^{3}}{m x y}
$$

12 Write $\frac{x+2}{8}+\frac{2 x}{3}$ as a single fraction in its simplest form.

$$
\frac{3 x+6}{24}+\frac{16 x}{24}
$$

$\qquad$


1 st

13 Write $\frac{x+7}{6}+\frac{x+4}{9}$ as a single fraction in its simplest form.

$$
\frac{3(x+7)}{18}+\frac{2(x+4)}{18}=\frac{3 x+21+2 x+8}{18}
$$

$$
\text { Answer } \frac{5 x+29}{18}
$$

14 Write $\frac{x+3}{4}-\frac{x+1}{5}$ as a single fraction in its simplest form.

$$
\begin{aligned}
\frac{5(x+3)}{20}-\frac{4(x+1)}{20}= & \frac{5(x+3)-4(x+1)}{20} \\
& =\frac{5 x+15-4 x-4}{20} \\
& \frac{x+11}{20}
\end{aligned}
$$

$15 \quad$ Write $\frac{2 x+3}{7}-\frac{x-4}{2}$ as a single fraction in its simplest form.

$$
\frac{2(2 x+3)}{14}-\frac{7(x-4)}{14}=\frac{2(2 x+3)-7(x-4)}{14}
$$

$$
=\frac{4 x+6-7 x+28}{14}
$$

Answer

$$
\frac{34-3 x}{14}
$$

16 Write $\frac{8}{x+2}+\frac{1}{2 x}$ as a single fraction in its simplest form.

$$
\frac{8(2 x)}{2 x(x+2)}+\frac{1(x+2)}{2 x(x+2)}=\frac{8(2 x)+(x+2)}{2 x(x+2)}
$$

$$
=\frac{16 x+x+2}{2 x^{2}+4 x}
$$

Answer

$$
\begin{aligned}
& \frac{17 x+2}{2 x^{2}+4}\left[\frac{17 x+2}{2 x(x+2)}\right. \\
& \text { fraction in its simplest form. } \\
& =\frac{10(x+5)+5(x+4)}{(x+4)(x+5)}
\end{aligned}
$$

$$
\left.\begin{array}{rl}
\frac{10(x+5)}{(x+4)(x+5)}+\frac{5(x+4)}{(x+4)(x+5)} & =\frac{10(x+5)+5(x+4)}{(x+4)(x+5)} \\
& =\frac{10 x+50+5 x+20}{(x+4)(x+5)} \\
\text { Answer } \frac{15 x+70}{x^{2}+9 x+20}\left[\frac{15 x+70}{(x+4)(x+5)}\right. & \text { also }
\end{array}\right]
$$

18 Write $\frac{9}{x+8}-\frac{5}{x-5}$ as a single fraction in its simplest form.

$$
\left.\begin{array}{rl}
\frac{9(x-5)}{(x+8)(x-5)}-\frac{5(x+8)}{(x+8)(x-5)} & =\frac{9(x-5)-5(x+8)}{(x+8)(x-5)} \\
& =\frac{9 x-45-5 x-40}{(x+8)(x-5)} \\
\text { Answer } \frac{4 x-85}{x^{2}+3 x-40} \quad\left[\frac{4 x-85}{(x+8)(x-5)}\right. & \text { is }
\end{array}\right]
$$

19 Write $\frac{5}{x-3}-\frac{3}{x+3}$ as a single fraction in its simplest form.
[3 marks]

$$
\frac{5(x+3)}{(x-3)(x+3)}-\frac{3(x-3)}{(x-3)(x+3)}=\frac{5(x+3)-3(x-3)}{(x-3)(x+3)}
$$

$$
=\frac{5 x+15-3 x+9}{(x-3)(x+3)}
$$

$$
\text { Answer } \frac{2 x+24}{x^{2}-9}\left[\frac{2 x+24}{(x+3)(x-3} \text { is } \text { or }\right]
$$

20 Write $\frac{x}{x-1}-\frac{2}{x+3}$ as a single fraction in its simplest form.
[3 marks]

$$
\frac{x(x+3)}{(x-1)(x+3)}-\frac{2(x-1)}{(x-1)(x+3)}=\frac{x(x+3)-2(x-1)}{(x-1)(x+3)}
$$

$$
=\frac{x^{2}+3 x-2 x+2}{(x-1)(x+3)}
$$

$$
\text { Answer } \frac{x^{2}+x+2}{x^{2}-2 x-3} \quad\left[\begin{array}{lc}
\frac{x^{2}+x+2}{(x-1)(x+3)} & \text { is } \\
\text { ok! }
\end{array}\right]
$$

21 Write $\frac{1}{2 x-3}-\frac{x}{3 x+5}$ as a single fraction in its simplest form.
[4 marks]

$$
\begin{aligned}
& \frac{\frac{1(3 x+5)}{(2 x-3)(3 x+5)}-\frac{x(2 x-3)}{(2 x-3)(3 x+5)}}{}=\frac{3 x+5-x(2 x-3)}{(2 x-3)(3 x+5)} \\
&=\frac{3 x+5-2 x^{2}+3 x}{(2 x-3)(3 x+5)} \\
& \text { Answer } \frac{6 x+5-2 x^{2}}{6 x^{2}+x-15}
\end{aligned}
$$

