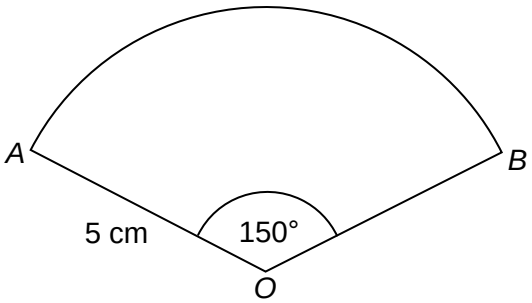
Sectors (Area and Arc Length)

SCAN ME

REVISE THIS TOPIC

1 *OAB* is a sector of a circle.



Not drawn accurately

1 (a) Work out the area of the sector.
Give your answer to 1 decimal place. **[2 marks]**

$\frac{150}{360} \times \pi \times 5^2$

$= 32.724923 47$

32.7

Answer 32.7 cm^2

1 (b) Work out the length of the arc *AB*.
Give your answer to 1 decimal place. **[2 marks]**

$\frac{150}{360} \times \pi \times 10$

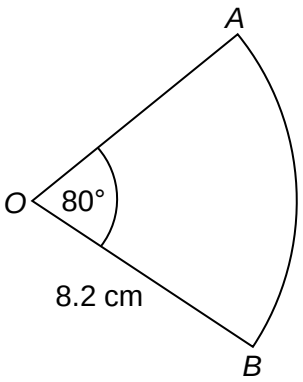
$= 13.089969 39$

13.1

Answer 13.1 cm

4

2 *OAB* is a sector of a circle.



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2 (a) Work out the area of the sector.
Give your answer to 1 decimal place. **[2 marks]**

$\frac{80}{360} \times \pi \times 8.2^2$

$= 46.942375 56$

46.9

Answer 46.9 cm^2

2 (b) Work out the length of the arc *AB*.
Give your answer to 1 decimal place. **[2 marks]**

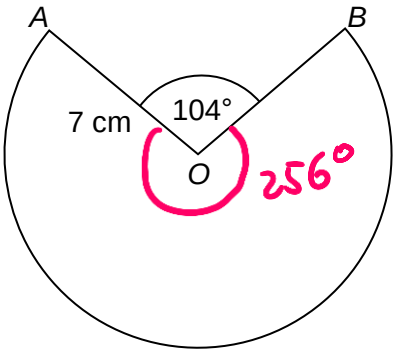
$\frac{80}{360} \times \pi \times 16.4$

$= 11.449359 89$

11.4

Answer 11.4 cm

3 *OAB* is a sector of a circle.



Not drawn accurately

360 − 104
= 256°

3 (a) Work out the area of the sector.
Give your answer to 1 decimal place. **[2 marks]**

$\frac{256}{360} \times \pi \times 7^2$

$= 109.4670507$

109.5

Answer _____ cm^2

3 (b) Work out the length of the arc *AB*.
Give your answer to 1 decimal place. **[2 marks]**

$\frac{256}{360} \times \pi \times 14$

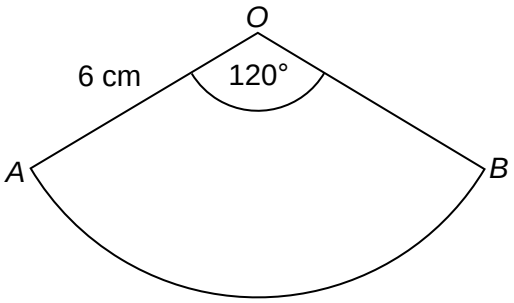
$= 31.2763002$

31.3

Answer _____ cm

8

4 *OAB* is a sector of a circle.



Not drawn accurately

4 (a) Work out the area of the sector.
Give your answer in terms of π **[2 marks]**

$\frac{120}{360} \times \pi \times 6^2$

$= \frac{1}{3} \times \pi \times 36$

Answer 12π cm^2

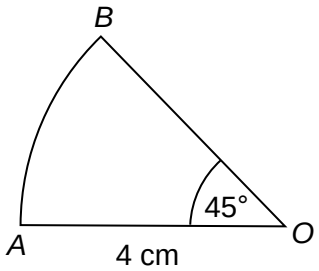
4 (b) Work out the length of the arc *AB*.
Give your answer in terms of π **[2 marks]**

$\frac{120}{360} \times \pi \times 12$

$= \frac{1}{3} \times \pi \times 12$

Answer 4π cm

5 *OAB* is a sector of a circle.



Not drawn accurately

5 (a) Work out the area of the sector.
Give your answer in terms of π **[2 marks]**

$\frac{45}{360} \times \pi \times 4^2$

$= \frac{1}{8} \times \pi \times 16$

Answer 2π cm^2

5 (b) Work out the length of the arc *AB*.
Give your answer in terms of π **[2 marks]**

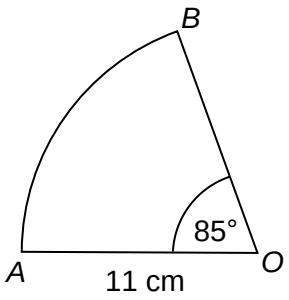
$\frac{45}{360} \times \pi \times 8$

$= \frac{1}{8} \times \pi \times 8$

Answer π cm

8

6 *OAB* is a sector of a circle.



Not drawn accurately

Work out the **perimeter** of the sector.
Give your answer to 1 decimal place. **[3 marks]**

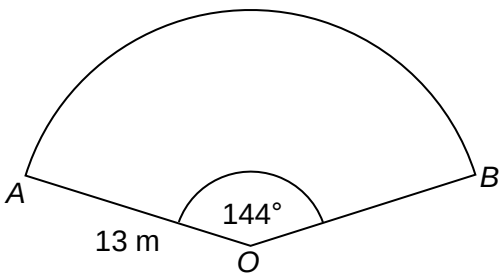
Arc length = $\frac{85}{360} \times \pi \times 22$

$= 16.31882851$

$16.3\ldots + 11 + 11 = 38.31882851$

Answer 38.3 cm

7 *OAB* is a sector of a circle.



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Work out the **perimeter** of the sector.
Give your answer to 1 decimal place. **[3 marks]**

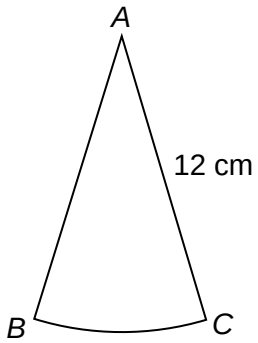
Arc length = $\frac{144}{360} \times \pi \times 26$

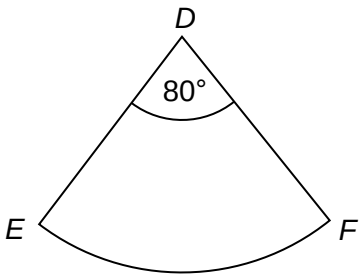
$= 32.67256360$

$32.6\ldots + 13 + 13 = 58.67256360$

Answer 58.7 m

8 *ABC and DEF* are sectors of different circles.





Not drawn accurately

AC : *DF* = 3 : 2
Angle *BAC* : Angle *EDF* = 2 : 5

Tick the box for the sector with the greater area.

☐ Sector *ABC* ☑ Sector *DEF*

Show working to support your answer. **[5 marks]**

AC : DF
3 : 2 (×4) → 12 : 8

BAC : EDF
2 : 5 (×16) → 32 : 80

Area ABC = $\frac{32}{360} \times \pi \times 12^2$

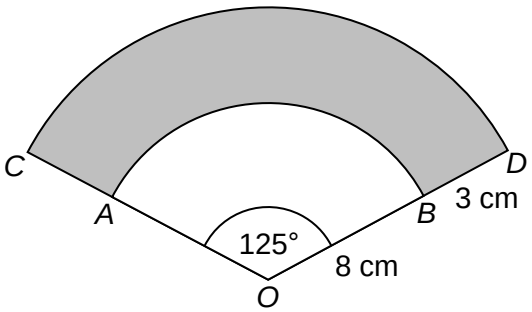
$= 40.21238597$

Area DEF = $\frac{80}{360} \times \pi \times 8^2$

$= 44.68042885$

11

9 *OAB* and *OCD* are sectors of circles with centre *O*.



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OB = 8 cm
BD = 3 cm

Work out the area of the shaded region.
Give your answer to 3 significant figures. **[4 marks]**

Area OCD = $\frac{125}{360} \times \pi \times 11^2$

$= 131.9905247$

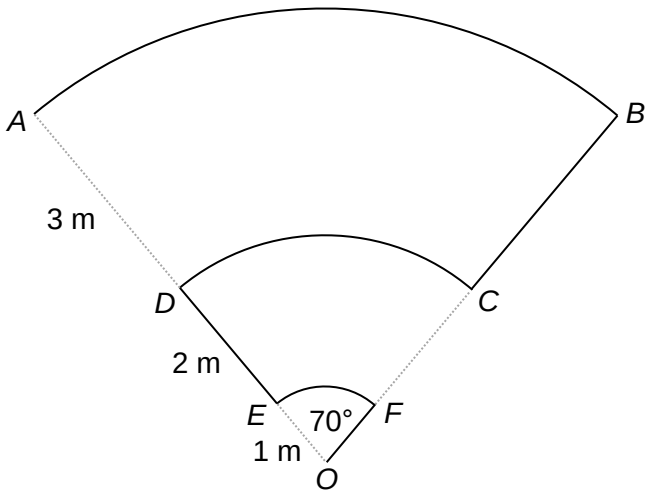
Area OAB = $\frac{125}{360} \times \pi \times 8^2$

$= 69.81317008$

$131.99... - 69.81... = 62.17735462$

Answer 62.2 cm^2

10 *OAB*, *ODC* and *OEF* are sectors of circles with centre *O*.



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OE = 1 m
ED = 2 m
DA = 3 m
Angle *AOB* = Angle *DOC* = Angle *EOF* = 70°

A robot starts at point *A* and follows the path *ABCDEFO*.

Work out the total distance that the robot travels.
Give your answer to 1 decimal place. **[4 marks]**

$AB = \frac{70}{360} \times \pi \times 12 = 7.330382858$

$CD = \frac{70}{360} \times \pi \times 6 = 3.665191429$

$EF = \frac{70}{360} \times \pi \times 2 = 1.221730476$

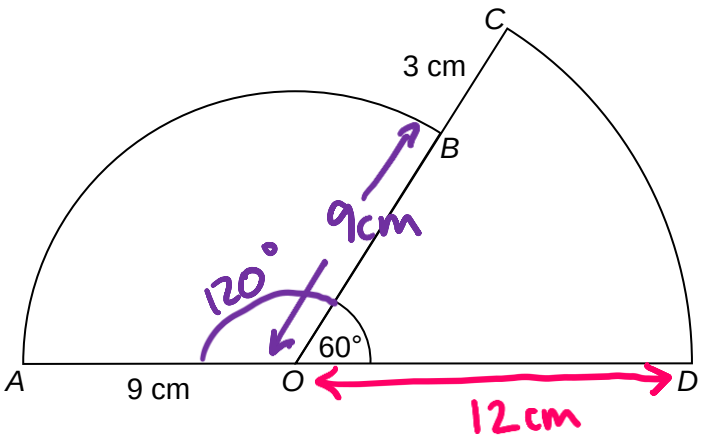
$7.33... + 3.66... + 1.22... + 3 + 2 + 1$
$= 18.217304 76$

Answer 18.2 m

8

Turn over ►

11 *OAB* and *OCD* are sectors of circles with centre *O*.



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AO = 9 cm
BC = 3 cm
Angle *COD* = 60°

AOB and *OBC* are straight lines.

Area of sector *OAB* – Area of sector *OCD* = $k\pi$ where k is an integer.

Work out the value of k.

[4 marks]

Area OAB $= \frac{120}{360} \times \pi \times 9^2$

$= \frac{1}{3} \times \pi \times 81$

$= 27\pi$

Area OCD $= \frac{60}{360} \times \pi \times 12^2$

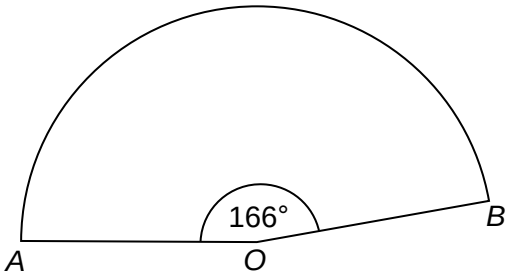
$= \frac{1}{6} \times \pi \times 144$

$= 24\pi$

$27\pi - 24\pi = 3\pi$

$k =$ 3

12 *OAB* is a sector of a circle.



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The area of the sector is 32 cm^2
Work out the radius of the sector.
Give your answer to 1 decimal place.

[3 marks]

$\frac{166}{360} \times \pi \times r^2 = 32$

$r^2 = \frac{32 \times 360}{166\pi}$

$r^2 = 22.089939\ldots$

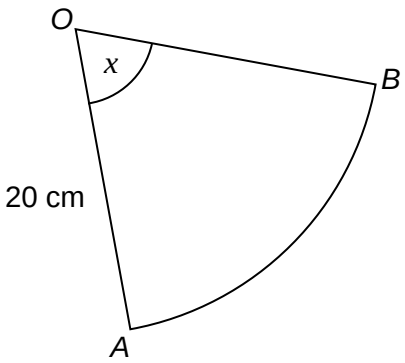
$r = \sqrt{22.08\ldots}$

4.7

Answer _____ cm

7

13 *OAB* is a sector of a circle.



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The length of arc *AB* is 22 cm
Work out the value of x.
Give your answer to the nearest degree.

[3 marks]

$\frac{x}{360} \times \pi \times 40 = 22$

$x = \frac{22 \times 360}{40\pi}$

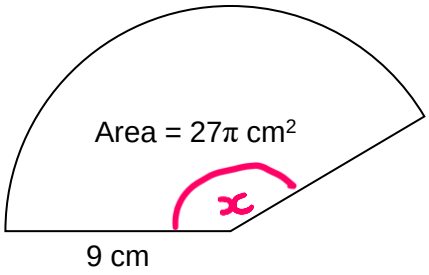
$x = 63.0253\ldots$

$x =$ 63 °

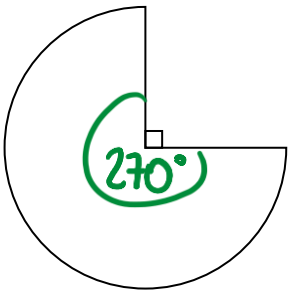
14 Here are two sectors from different circles.

Not drawn accurately

Sector **A**



Sector **B**



The length of the arc of sector **B** = 2 × the length of the arc of sector **A**

Work out the area of sector **B**
Give your answer in terms of π

[6 marks]

$\frac{x}{360} \times \pi \times 9^2 = 27\pi$

$\frac{81x\pi}{360} = 27\pi$

$\frac{9x}{40} = 27$

$x = \frac{27 \times 40}{9}$

$x = 120^\circ$

$\text{Arc}_A = \frac{120}{360} \times \pi \times 18$

$= \frac{1}{3} \times \pi \times 18$

$= 6\pi$

$\text{Arc}_B = 12\pi$

$\frac{270}{360} \times \pi \times d = 12\pi$

$\frac{3}{4}\pi d = 12\pi$

$d = \frac{12 \times 4}{3}$

$d = 16$

$r = 8$

$\frac{270}{360} \times \pi \times 8^2$

$= \frac{3}{4} \times \pi \times 64$

$= 48\pi$

Answer 48π cm²

9