



# Measures of Central Tendency



REVISE THIS TOPIC

CHECK YOUR ANSWERS



1 A school gives all 120 Year 7 students and all 130 Year 8 students the same maths test.

The maths department wishes to compare the test scores of students in Year 7 ( $x\%$ ) with the test scores of students in Year 8 ( $y\%$ ).

$$\sum x = 8160 \qquad \sum y = 8190$$

(a) By calculating the mean test score for each year group, compare the test scores of students in Year 7 with those in Year 8. (2)

It is found that some of the Year 7 students cheated in the test and each had scored 100%

(b) (i) Suggest another measure of central tendency that the maths department could use to compare the test scores in this case. (1)

(ii) Explain why the measure you have suggested would be more suitable than the mean. (1)

The school also tests Year 9 students.

The following table summarises the test scores,  $T\%$ , for all of the Year 9 students.

Test Score, $T\%$	$0 \leq T < 20$	$20 \leq T < 40$	$40 \leq T < 60$	$60 \leq T < 80$	$80 \leq T < 100$
Number of students, $f$	1	17	52	66	44

(c) Work out an estimate for the mean test score for Year 9 students. (2)

(Total for Question 1 is 6 marks)



2 The following table summarises heights,  $y$  cm to the nearest centimetre, of the female athletes at an athletics club.

Height ( $y$ cm)	$160 \leq y < 170$	$170 \leq y < 180$	$180 \leq y < 190$	$190 \leq y < 200$
Number of athletes ( $f$ )	3	7	7	8

- (a) State the modal class for the heights of the female athletes. (1)
- (b) Work out the class interval containing the median female height. (1)
- (c) Work out an estimate for the mean height of the female athletes. (2)

For the heights,  $x$  cm to the nearest centimetre, of the male athletes at the club

$$\sum x = 6615 \quad n = 35$$

- (d) Use this data, and your answer to part (c) to estimate the mean height of all of the male and female athletes at the athletics club. (2)

(Total for Question 2 is 6 marks)

3 The following tables summarises the annual salaries, £ $S$  to the nearest pound, of teachers at a multi-academy trust.

Annual Salary (£ $S$ )	Frequency ( $f$ )
$30,000 \leq S < 50,000$	84
$50,000 \leq S < 70,000$	18
$70,000 \leq S < 90,000$	9
$90,000 \leq S < 110,000$	3
$110,000 \leq S < 200,000$	1

- (a) Work out the class interval containing the median annual salary. (1)
- (b) Work out an estimate, to the nearest pound, for the mean annual salary all of the staff. (1)
- (c) Explain why your answer to part (b) is an estimate. (1)

It is found that the CEO of the multi-academy trust has an annual salary of £195,000 (yes really)

- (d) Explain what effect, if any, will this information have on
- (i) your answer to part (a)
- (ii) your answer to part (b) (2)

(Total for Question 3 is 5 marks)



4 On Monday 12 students were late to school.  
The number of minutes late  $L$ , to the nearest minute, of the first 8 students are shown below.

Student	A	B	C	D	E	F	G	H
Lateness ( $L$ minutes)	1	2	3	3	4	6	8	9

- (a) State the modal number of minutes late for the first 8 students. (1)
- (b) Work out the median number of minutes late for the first 8 students. (1)
- (c) Work out the mean number of minutes late for the first 8 students. (1)

Any student who is 10 or more minutes late receives a detention.  
On Monday 4 students received a detention for being late.

The mean number of minutes late for all 12 students on Monday was 10.5 minutes.

- (d) Work out the mean of minutes late for the 4 students who received a detention on Monday. (2)

(Total for Question 4 is 5 marks)

5 The table below summarises the number of fillings of 20 patients randomly sampled at a dentist.

Number of Fillings	0	1	2	3	4	5	6
Frequency ( $f$ )	7	4	3	3	0	2	1

- (a) State the modal number of fillings. (1)
- (b) Work out the median number of fillings. (1)
- (c) Work out the mean number of fillings. (2)

Another patient is added to the sample. They have 2 fillings.

- (d) Explain what affect, if any, this will have on
- (i) your answer to part (a)
- (ii) your answer to part (b)
- (iii) your answer to part (c) (3)

(Total for Question 5 is 7 marks)



6 Mark's internet provider claims that the average internet speed that he will receive will be at least 100 Mbps.

Mark tests his internet speed  $S$ , to the nearest Mbps, at 12 different times during the day. The table below summarises the results.

<b>Internet Speed (<math>S</math> Mbps)</b>	90-99	100-109	110-119	120-129
<b>Frequency (<math>f</math>)</b>	4	6	1	1

- (a) Work out an estimate of the mean internet speed.  
Give your answer to 4 significant figures. (2)
- (b) Explain why your answer to part (a) is only an estimate. (1)
- (c) Does your answer to part (a) support the claim made by the internet provider? (1)

Mark works out the exact value for the mean using his recorded values.

- (d) Is it possible that Mark's mean internet speed is below 100 Mbps?  
Give a reason for your answer. (2)

**(Total for Question 6 is 6 marks)**

7 The speeds,  $S$  mph to the nearest mph, of some vehicles on a motorway are recorded.

<b>Lane of Motorway</b>	Lane 1	Lane 2	Lane 3
<b>Number of Vehicles</b>	124	148	165
<b>Mean Speed (mph)</b>	55.2	67.8	71.3

Work out the mean speed of all vehicles across all lanes of the motorway.  
Give your answer to 3 significant figures. (2)

**(Total for Question 7 is 2 marks)**

8 The following tables summarises the ages,  $A$  years, of people taking a driving test at a test centre.

<b>Age (<math>A</math> years)</b>	10-19	20-29	30-39	40-49	50-59	60-69
<b>Frequency (<math>f</math>)</b>	21	4	1	2	1	1

- (a) Work out the class interval containing the median age. (1)
- (b) Work out an estimate for the mean age of the people taking a driving test at the test centre. (2)

The minimum age for taking a driving test is 17 years old.

- (c) Comment on whether the true mean age of the drivers at the test centre likely to be different to your answer to part (b). Give a reason for your answer. (1)

**(Total for Question 8 is 4 marks)**

