

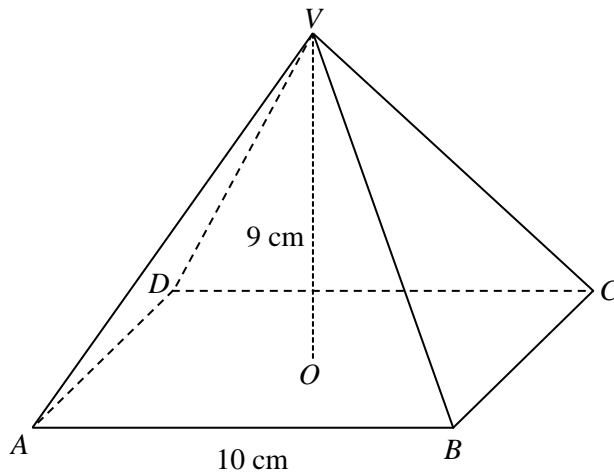
# Volume and Surface Area of Pyramids



REVISE THIS  
TOPIC



- 1  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.



Work out the volume of the pyramid.

$$\begin{aligned} & \frac{1}{3} \times 10 \times 10 \times 9 \\ &= \frac{1}{3} \times 900 \\ &= 300 \end{aligned}$$

300

.....cm<sup>3</sup>  
(Total for Question 1 is 2 marks)

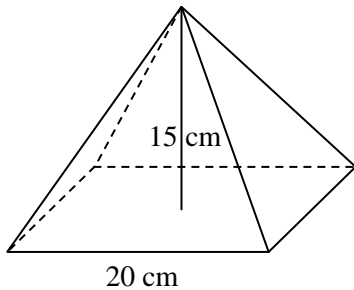


1

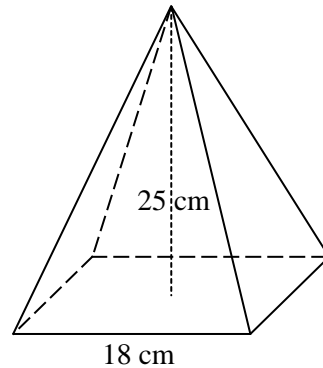


2 Here are two square based pyramids.

**Pyramid A**



**Pyramid B**



The volume of **Pyramid A** is less than the volume of **Pyramid B**.

Work out how much less.

$$\frac{1}{3} \times 20 \times 20 \times 15 = 2000$$

$$\frac{1}{3} \times 18 \times 18 \times 25 = 2700$$

$$2700 - 2000 = 700$$

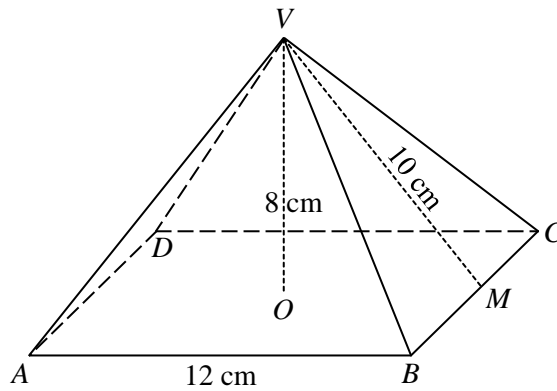
700

.....cm<sup>3</sup>

(Total for Question 2 is 4 marks)



- 3  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $BC$ .



- (a) Work out the volume of the pyramid.

$$\frac{1}{3} \times 12 \times 12 \times 8 = 384$$

$$\underline{\quad 384 \quad} \text{cm}^3$$

(2)

- (b) Work out the surface area of the pyramid.

$$12 \times 12 = 144$$

$$\frac{1}{2} \times 12 \times 10 = 60$$

$$60 \times 4 = 240$$

$$240 + 144 = 384$$

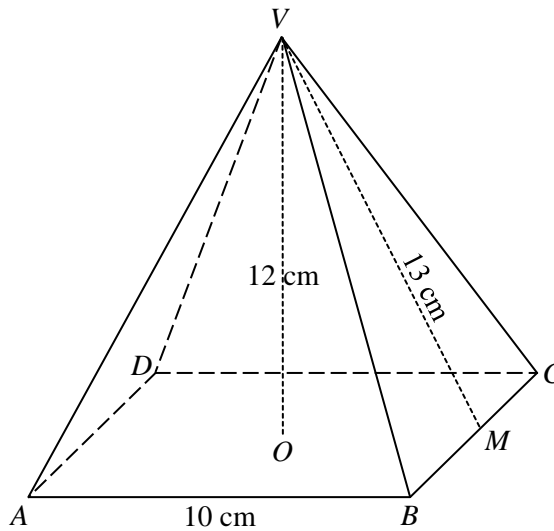
$$\underline{\quad 384 \quad} \text{cm}^2$$

(4)

(Total for Question 3 is 6 marks)



- 4  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $BC$ .



- (a) Work out the volume of the pyramid.

$$\frac{1}{3} \times 10 \times 10 \times 12 = 400$$

$$\underline{\hspace{10em} 400 \hspace{10em}} \text{cm}^3$$

(2)

- (b) Work out the surface area of the pyramid.

$$10 \times 10 = 100$$

$$\frac{1}{2} \times 10 \times 13 = 65$$

$$65 \times 4 = 260$$

$$260 + 100 = 360$$

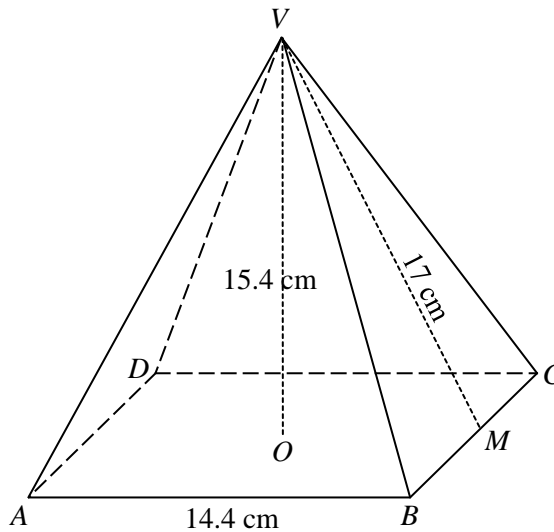
$$\underline{\hspace{10em} 360 \hspace{10em}} \text{cm}^2$$

(4)

(Total for Question 4 is 6 marks)



- 5  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $BC$ .



- (a) Work out the volume of the pyramid.  
 Give your answer to the nearest integer.

$$\frac{1}{3} \times 14.4 \times 14.4 \times 15.4 = 1064.448$$

$$\underline{\hspace{10em} 1064 \hspace{10em}} \text{cm}^3$$

(2)

- (b) Work out the surface area of the pyramid.  
 Give your answer to the nearest integer.

$$14.4 \times 14.4 = 207.36$$

$$\frac{1}{2} \times 14.4 \times 17 = 122.4$$

$$122.4 \times 4 = 489.6$$

$$489.6 + 207.36 = 696.96$$

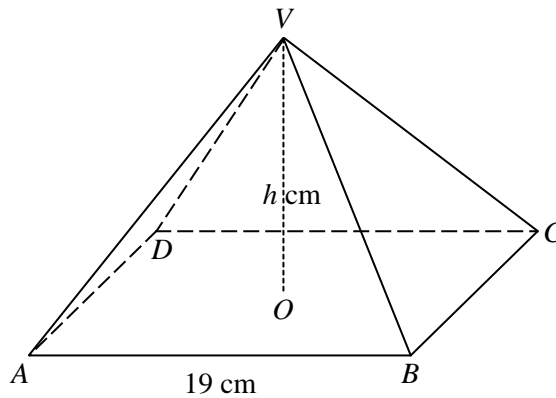
$$\underline{\hspace{10em} 697 \hspace{10em}} \text{cm}^2$$

(4)

(Total for Question 5 is 6 marks)



6  $VABCD$  is a squared-based pyramid.



The volume of the pyramid is  $1500 \text{ cm}^3$

Work out the value of  $h$ , the perpendicular height of the pyramid.  
Give your answer to 1 decimal place.

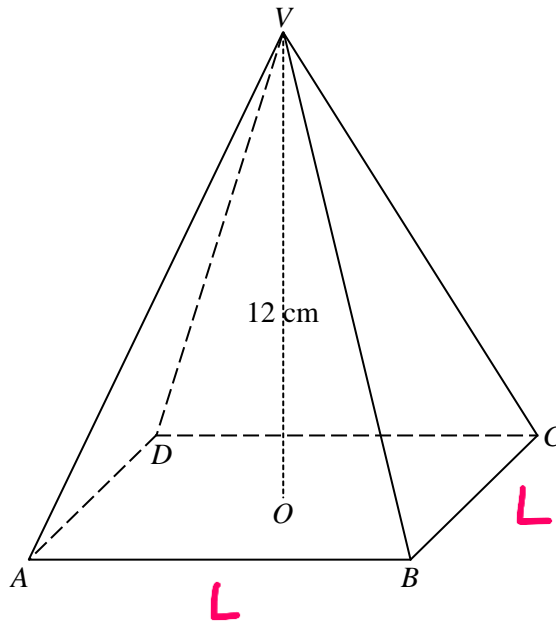
$$\begin{aligned}
 \frac{1}{3} \times 19 \times 19 \times h &= 1500 \\
 \frac{361h}{3} &= 1500 \\
 \times 3 \downarrow & \quad \quad \quad \downarrow \times 3 \\
 361h &= 4500 \\
 \div 361 \downarrow & \quad \quad \quad \downarrow \div 361 \\
 h &= 12.46537\dots
 \end{aligned}$$

$h = \underline{12.5} \text{ cm}$

(Total for Question 6 is 3 marks)



- 7  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.



The volume of the pyramid is  $300 \text{ cm}^3$

Work out the length of side  $AB$ .

Give your answer to 1 decimal place.

$$\begin{aligned}
 \frac{1}{3} \times L \times L \times 12 &= 300 \\
 4L^2 &= 300 \\
 L^2 &= 75 \\
 L &= \sqrt{75} \\
 L &= 8.66025\dots
 \end{aligned}$$

8.7

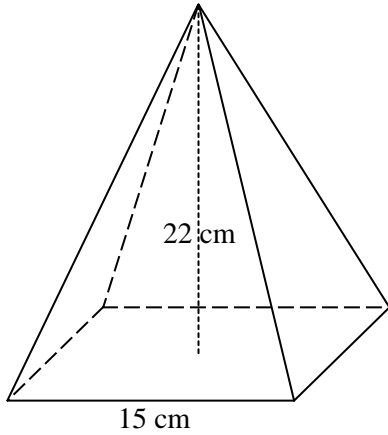
.....cm

(Total for Question 7 is 4 marks)

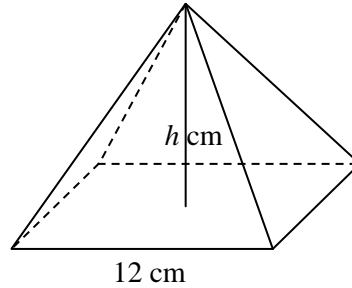


- 8  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.

Pyramid A



Pyramid B



Volume of **Pyramid A** =  $2 \times$  Volume of **Pyramid B**

Work out the value of  $h$ , the perpendicular height of **Pyramid B**.  
 Give your answer to 1 decimal place.

$$\frac{1}{3} \times 15 \times 15 \times 22 = 1650$$

$$1650 \div 2 = 825$$

$$\frac{1}{3} \times 12 \times 12 \times h = 825$$

$$48h = 825$$

$$h = 17.1875$$

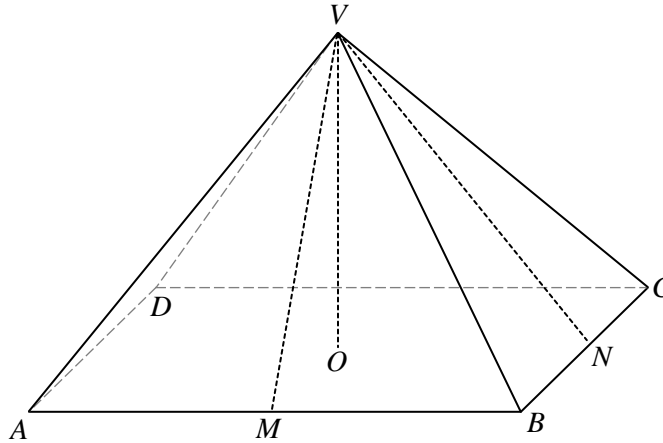
$$h = \underline{17.2} \text{ cm}$$

(Total for Question 8 is 5 marks)





- 9 Here  $VABCD$  is a pyramid with rectangular base  $ABCD$ .  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $AB$ .  
 $N$  is the midpoint of  $BC$ .



$$VA = VB = VC = VD$$

$$AB = 36 \text{ cm}$$

$$BC = 14 \text{ cm}$$

$$VO = 24 \text{ cm}$$

$$VM = 25 \text{ cm}$$

$$VN = 30 \text{ cm}$$

- (a) Work out the volume of the pyramid.

$$\frac{1}{3} \times 36 \times 14 \times 24 = 4032$$

$$\underline{\quad 4032 \quad} \text{cm}^3$$

(2)



(b) Work out the surface area of the pyramid.

$$36 \times 14 = 504$$

$$\frac{1}{2} \times 36 \times 25 = 450$$

$$\frac{1}{2} \times 14 \times 30 = 210$$

$$504 + 450 + 450 + 210 + 210 = 1824$$

1824

.....cm<sup>2</sup>

(4)

(Total for Question 9 is 6 marks)

