

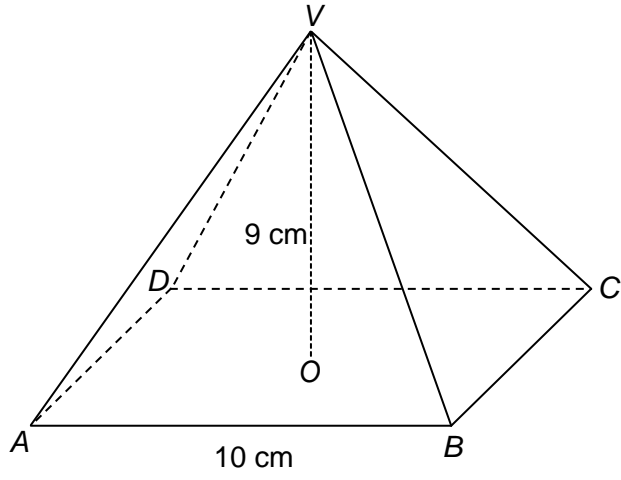


# Volume and Surface Area of Pyramids



REVISE THIS TOPIC

1 *VABCD* is a squared-based pyramid.  
*VO* is the perpendicular height of the pyramid.



$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$

Work out the volume of the pyramid. [2 marks]

$\frac{1}{3} \times 10 \times 10 \times 9$   
 $= \frac{1}{3} \times 900$   
 $= 300$

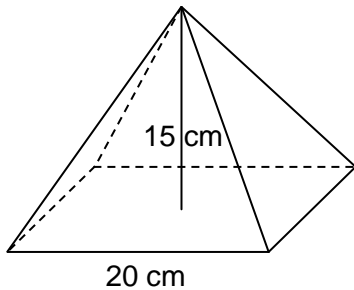
Answer 300 cm<sup>3</sup>



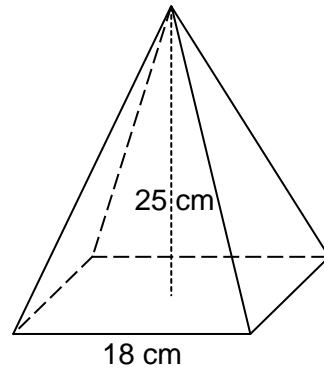


2 Here are two square based pyramids.

Pyramid A



Pyramid B



$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$

The volume of **Pyramid A** is less than the volume of **Pyramid B**.

Work out how much less.

[4 marks]

$$\frac{1}{3} \times 20 \times 20 \times 15 = 2000$$

$$\frac{1}{3} \times 18 \times 18 \times 25 = 2700$$

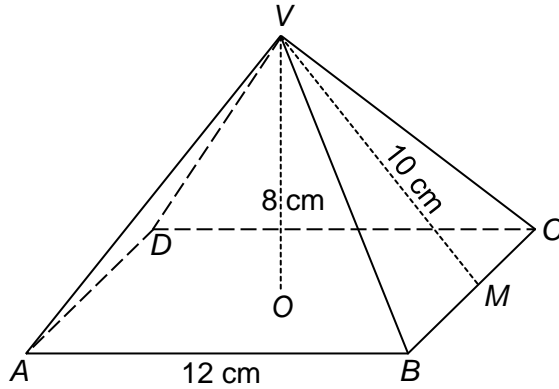
$$2700 - 2000 = 700$$

Answer 700 cm<sup>3</sup>





- 3 *VABCD* is a squared-based pyramid.  
*VO* is the perpendicular height of the pyramid.  
*M* is the midpoint of *BC*.



$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$

- 3 (a) Work out the volume of the pyramid. [2 marks]

$$\frac{1}{3} \times 12 \times 12 \times 8 = 384$$

Answer 384 cm<sup>3</sup>

- 3 (b) Work out the surface area of the pyramid. [4 marks]

$$12 \times 12 = 144$$

$$\frac{1}{2} \times 12 \times 10 = 60$$

$$60 \times 4 = 240$$

$$240 + 144 = 384$$

Answer 384 cm<sup>2</sup>

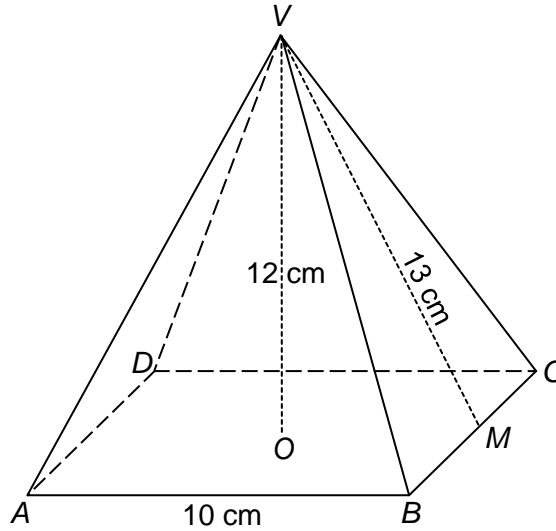
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$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$





- 4  $VABCD$  is a squared-based pyramid.  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $BC$ .



- 4 (a) Work out the volume of the pyramid. [2 marks]

$$\frac{1}{3} \times 10 \times 10 \times 12 = 400$$

Answer 400 cm<sup>3</sup>

- 4 (b) Work out the surface area of the pyramid. [4 marks]

$$10 \times 10 = 100$$

$$\frac{1}{2} \times 10 \times 13 = 65$$

$$65 \times 4 = 260$$

$$260 + 100 = 360$$

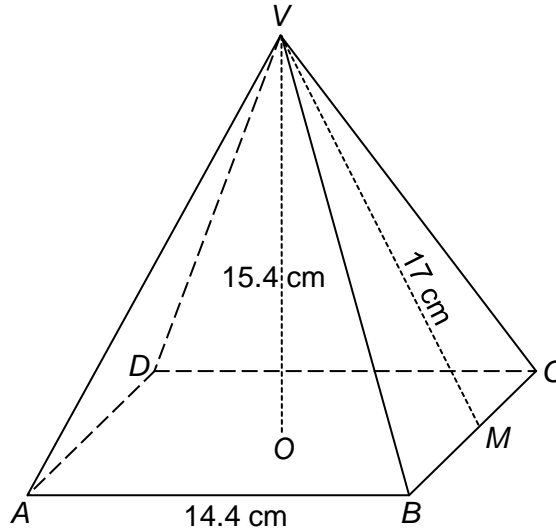
Answer 360 cm<sup>2</sup>



Volume of pyramid =  $\frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$



- 5 *VABCD* is a squared-based pyramid.  
*VO* is the perpendicular height of the pyramid.  
*M* is the midpoint of *BC*.



- 5 (a) Work out the volume of the pyramid.  
 Give your answer to the nearest integer. [2 marks]

$$\frac{1}{3} \times 14.4 \times 14.4 \times 15.4 = 1064.448$$

Answer 1064 cm<sup>3</sup>

- 5 (b) Work out the surface area of the pyramid.  
 Give your answer to the nearest integer. [4 marks]

$$14.4 \times 14.4 = 207.36$$

$$\frac{1}{2} \times 14.4 \times 17 = 122.4$$

$$122.4 \times 4 = 489.6$$

$$489.6 + 207.36 = 696.96$$

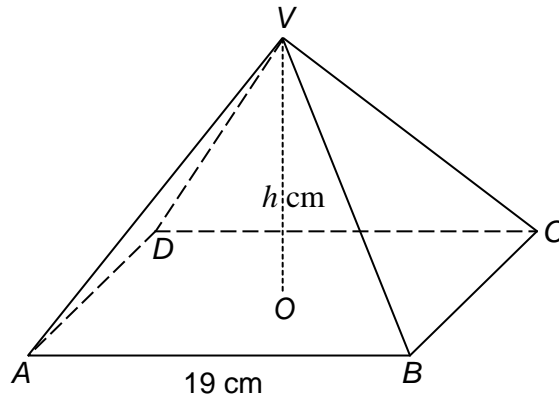
Answer 697 cm<sup>2</sup>



Volume of pyramid =  $\frac{1}{3} \times$  area of base  $\times$  perpendicular height



6 *VABCD* is a squared-based pyramid.



The volume of the pyramid is  $1500 \text{ cm}^3$

Work out the value of  $h$ , the perpendicular height of the pyramid.

Give your answer to 1 decimal place.

[3 marks]

$$\frac{1}{3} \times 19 \times 19 \times h = 1500$$

$$\frac{361h}{3} = 1500$$

$\times 3$

$\times 3$

$\div 361$

$\div 361$

$$361h = 4500$$

$\div 361$

$$h = 12.46537\dots$$

$h =$  12.5 cm

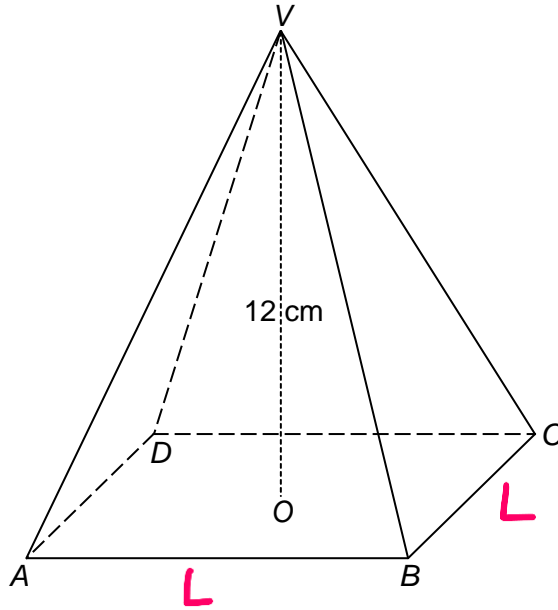


Volume of pyramid =  $\frac{1}{3} \times$  area of base  $\times$  perpendicular height



7

VABCD is a squared-based pyramid.  
VO is the perpendicular height of the pyramid.



The volume of the pyramid is  $300 \text{ cm}^3$

Work out the length of side AB.  
Give your answer to 1 decimal place.

[4 marks]

$$\frac{1}{3} \times L \times L \times 12 = 300$$

$$4L^2 = 300$$

$$L^2 = 75$$

$$L = \sqrt{75}$$

$$L = 8.66025\dots$$

Answer 8.7 cm



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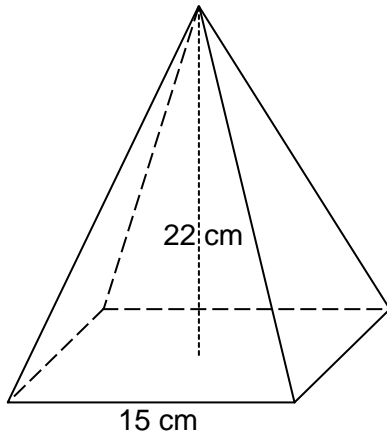
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Volume of pyramid =  $\frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$

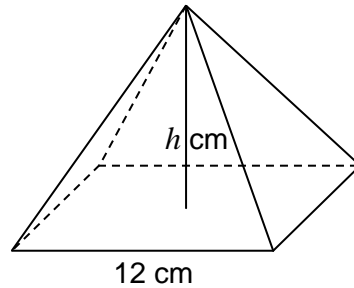


8 Here are two square based pyramids.

Pyramid A



Pyramid B



$$\text{Volume of Pyramid A} = 2 \times \text{Volume of Pyramid B}$$

Work out the value of  $h$ , the perpendicular height of Pyramid B. Give your answer to 1 decimal place.

[5 marks]

$$\frac{1}{3} \times 15 \times 15 \times 22 = 1650$$

$$1650 \div 2 = 825$$

$$\frac{1}{3} \times 12 \times 12 \times h = 825$$

$$48h = 825$$

$$h = 17.1875$$

$$h = 17.2 \text{ cm}$$

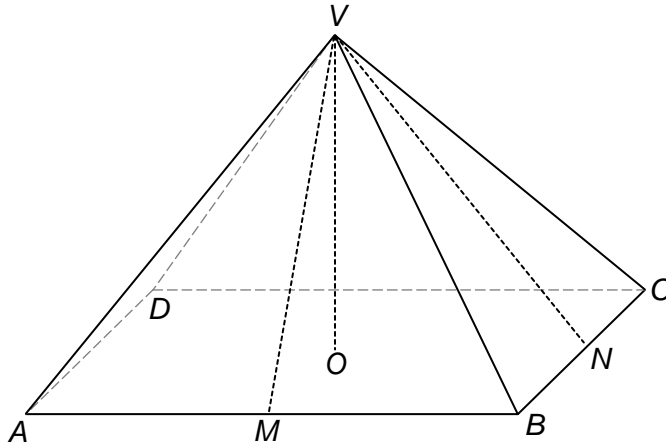


$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$





- 9 Here  $VABCD$  is a pyramid with rectangular base  $ABCD$ .  
 $VO$  is the perpendicular height of the pyramid.  
 $M$  is the midpoint of  $AB$ .  
 $N$  is the midpoint of  $BC$ .



$$VA = VB = VC = VD$$

- $AB = 36 \text{ cm}$
- $BC = 14 \text{ cm}$
- $VO = 24 \text{ cm}$
- $VM = 25 \text{ cm}$
- $VN = 30 \text{ cm}$

$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$

- 9 (a) Work out the volume of the pyramid. [2 marks]

$$\frac{1}{3} \times 36 \times 14 \times 24 = 4032$$

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Answer 4032 cm<sup>3</sup>

$\frac{2}{2}$



$$\text{Volume of pyramid} = \frac{1}{3} \times \text{area of base} \times \text{perpendicular height}$$

Turn over ►



9 (b) Work out the surface area of the pyramid.

[4 marks]

$$36 \times 14 = 504$$

$$\frac{1}{2} \times 36 \times 25 = 450$$

$$\frac{1}{2} \times 14 \times 30 = 210$$

$$504 + 450 + 450 + 210 + 210 = 1824$$

Answer 1824 cm<sup>2</sup>

