Quadratic Inequalities

REVISE THIS TOPIC

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1 Solve }\mp@subsup{x}{}{2}+7x+10<
    (x+2)(x+5)<0
    C.V. }x=-
        x=-5
            -5<x<-2
            (Total for Question 1 is 2 marks)
2 Solve }\mp@subsup{x}{}{2}-9x+20>
    (x-5)(x-4)>0
    C.v. }x=
                x=4
                    \(Total for Question 2 is 2 marks)
3 Solve \(x^{2}+2 x-15<0\)
\[
(x+5)(x-3)<0
\]
CV.
\[
\begin{aligned}
& x=-5 \\
& x=3
\end{aligned}
\]
\[
-5<x<3
\]
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4 Solve }\mp@subsup{x}{}{2}+x-12>
(x+4)(x-3)>0
C.V. }x=-
\[
x=3
\]
\(x<-4\) or \(x>3\) (Total for Question 4 is 2 marks)
5 Solve \(x^{2}-2 x-24 \leq 0\)
\[
\begin{gathered}
(x-6)(x+4) \leqslant 0 \\
\text { c.v. } x=6
\end{gathered}
\]
\[
x=-4 \quad-4 \leqslant x \leqslant 6
\]
6 Solve \(x^{2}-17 x+30 \geq 0\)
\[
(x-2)(x-15) \geqslant 0
\]
CV. \(x=2\)
\[
x=15
\]
```

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7 Solve \(x^{2}-25 \leq 0\)
\[
\begin{gathered}
(x+5)(x-5) \leqslant 0 \\
\text { C.v. } x=-5 \\
x=5
\end{gathered}
\]
\[
\begin{aligned}
& 8 \text { Solve } 2 x^{2}-7 x-15>0 \\
& (2 x+3)(x-5)>0 \\
& \text { C.v. } x=-\frac{3}{2} \\
& x=5 \\
& x<-\frac{3}{2} \text { or } x>5 \\
& \text { (Total for Question } 8 \text { is } \mathbf{3} \text { marks) } \\
& (3 x-1)(x+6) \leqslant 0 \\
& \text { C.V. } x=1 / 3 \\
& x=-6 \quad-6 \leq x \leq \frac{1}{3} \\
& (5 x-3)(x-2) \geqslant 0 \\
& \text { C.V. } x=\frac{3}{5} \\
& x=2 \\
& x \leq \frac{3}{5} \text { or } x \geqslant 2 \\
& 2 x^{2}+17 x+21<0 \\
& (2 x+3)(x+7)<0 \\
& \text { c.v. } x=-\frac{3}{2} \\
& x=-7 \quad-7<x<-3 / 2
\end{aligned}
\]

\section*{- \(\mathrm{c}^{\prime}\) (O) @1stclassmaths}

12 (a) Solve \(x^{2}-2 x-8<0\)
\[
\begin{gathered}
(x-4)(x+2)<0 \\
\text { C.V. } x=4 \\
x=-2
\end{gathered}
\]

(2)
(b) Show the solution to \(x^{2}-2 x-8<0\) on the number line below.


13 (a) Solve \(x^{2}-7 x+10 \leq 0\)
\[
\begin{gathered}
(x-5)(x-2) \leqslant 0 \\
\text { C.V. } x=5 \\
x=2
\end{gathered}
\]
\(2 \leqslant x \leqslant 5\)
(2)
(b) Show the solution to \(x^{2}-7 x+10 \leq 0 \quad\) on the number line below.


14 Find a set of possible values of \(x\) for which
\[
\begin{array}{rlr}
4 x-5<19 & (x-10)(x+2)<0 \\
4 x<24 & \text { c.v. } x=10 \\
x & x 6 & -2<-2 \\
& -2<10
\end{array}
\]
both are true when \(-2<x<6\)

(Total for Question 14 is 4 marks)
15 Find a set of possible values of \(x\) for which
\[
\begin{aligned}
& 6 x+1>16 \\
& 6 x>15(x-6)(x-2)<0 \\
& x>\frac{15}{6} \text { CV. } x=6 \\
& x=2 \\
& 2<x<6
\end{aligned}
\]
\[
x>\frac{5}{2}
\]
both are true when \(\frac{5}{2}<x<6\)
\(\frac{5}{2}<x<6\)
(Total for Question 15 is 4 marks)

16 Find a set of possible values of \(x\) for which
\[
\begin{aligned}
& x^{2}-11 x+10<0 \quad \text { and } \quad 2 x^{2}+3 x-20<0 \\
& (x-10)(x-1)<0 \quad(2 x-5)(x+4)<0 \\
& \text { C. } x=10 \\
& x=1 \\
& 1<x<10 \quad-4<x<\frac{5}{2}
\end{aligned}
\]
both are true when \(1<x<\frac{5}{2}\)

17 Find a set of possible values of \(x\) for which
\[
\begin{array}{ll}
\begin{array}{ll}
x^{2}-9 \geq 0 \quad \text { and } \quad 2 x^{2}-13 x+15<0 \\
(x+3)(x-3) \geqslant 0 & (2 x-3)(x-5)<0 \\
\text { C.v } x=-3 & \text { C.V. } x=\frac{3}{2} \\
x=3 & x=5
\end{array} \\
x \leqslant-3 \text { or } x \geqslant 3 & \frac{3}{2}<x<5
\end{array}, \begin{array}{ll}
\text { both true when } & 3 \leqslant x<5
\end{array}
\]```

