



Recurring Decimals to Fractions



REVISE THIS
TOPIC



- 1 Convert $0.\dot{5}$ to a fraction giving your answer in its simplest form. [2 marks]

$$10x = 5.5555...$$

$$x = 0.5555...$$

$$9x = 5$$

$$x = \frac{5}{9}$$

$$\frac{5}{9}$$

Answer _____

- 2 Convert $0.\dot{7}\dot{1}$ to a fraction giving your answer in its simplest form. [2 marks]

$$100x = 71.717171...$$

$$x = 0.717171...$$

$$99x = 71$$

$$x = \frac{71}{99}$$

$$\frac{71}{99}$$

Answer _____





- 3 Convert $0.\dot{4}\dot{5}$ to a fraction giving your answer in its simplest form. [2 marks]

$$100x = 45.454545...$$

$$x = 0.454545...$$

$$99x = 45$$

$$x = \frac{45}{99}$$

$$\frac{45}{99} = \frac{5}{11}$$

Answer

$$\frac{5}{11}$$

- 4 Convert $0.\dot{2}\dot{1}\dot{4}$ to a fraction giving your answer in its simplest form. [3 marks]

$$1000x = 214.214214...$$

$$x = 0.214214...$$

$$999x = 214$$

$$x = \frac{214}{999}$$

Answer

$$\frac{214}{999}$$

- 5 Convert $0.\dot{3}\dot{2}\dot{4}$ to a fraction giving your answer in its simplest form. [3 marks]

$$1000x = 324.324324...$$

$$x = 0.324324...$$

$$999x = 324$$

$$x = \frac{324}{999}$$

$$\frac{324}{999} = \frac{36}{111} = \frac{12}{37}$$

Answer

$$\frac{12}{37}$$





- 6 Convert $0.\dot{5}3$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 100x = 53.3333 \\
 - 10x = 5.3333 \dots \\
 \hline
 x = 0.5333 \dots \\
 90x = 48 \\
 x = \frac{48}{90} \\
 \frac{48}{90} = \frac{8}{15}
 \end{array}$$

Answer $\frac{8}{15}$

- 7 Convert $0.12\dot{4}$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 1000x = 124.4444 \dots \\
 - 100x = 12.4444 \dots \\
 \hline
 x = 0.124444 \dots \\
 900x = 112 \\
 x = \frac{112}{900} \\
 \frac{112}{900} = \frac{28}{225}
 \end{array}$$

Answer $\frac{28}{225}$

- 8 Convert $0.4\dot{2}\dot{3}$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 1000x = 423.232323 \dots \\
 - 10x = 4.232323 \dots \\
 \hline
 x = 0.4232323 \dots \\
 990x = 419 \\
 x = \frac{419}{990}
 \end{array}$$

Answer $\frac{419}{990}$





- 9 Convert $0.\dot{0}3\dot{8}$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 1000x = 38.383838383 \dots \\
 - 10x = 0.383838383 \dots \\
 \hline
 x = 0.038383838 \dots \\
 \hline
 990x = 38 \\
 x = \frac{38}{990}
 \end{array}$$

$$\frac{38}{990} = \frac{19}{495}$$

Answer

$$\frac{19}{495}$$

- 10 Convert $3.\dot{6}\dot{2}$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 100x = 362.62626262 \dots \\
 x = 3.62626262 \dots \\
 \hline
 99x = 359 \\
 x = \frac{359}{99}
 \end{array}$$

$$\frac{359}{99}$$

Answer

- 11 Convert $0.3\dot{1}6\dot{1}$ to a fraction giving your answer in its simplest form. [3 marks]

$$\begin{array}{r}
 10000x = 3161.161161161 \dots \\
 - 10x = 3.161161161 \dots \\
 \hline
 x = 0.3161161161 \dots \\
 \hline
 9990x = 3158 \\
 x = \frac{3158}{9990}
 \end{array}$$

$$\frac{3158}{9990} = \frac{1579}{4995}$$

$$\frac{1579}{4995}$$

Answer





12

Work out $0.\dot{6}8 - 0.2\dot{7}$

[5 marks]

Give your answer as a fraction in its simplest form.

$$100x = 68.\dot{8}8888 \dots$$

$$100y = 27.\dot{7}7777 \dots$$

$$10x = 6.\dot{8}8888 \dots$$

$$10y = 2.\dot{7}7777 \dots$$

$$x = 0.\dot{6}8888 \dots$$

$$y = 0.2\dot{7}777 \dots$$

$$90x = 62$$

$$90y = 25$$

$$x = \frac{62}{90}$$

$$y = \frac{25}{90}$$

$$\frac{62}{90} - \frac{25}{90} = \frac{37}{90}$$

Answer

$$\frac{37}{90}$$

13

Work out $0.5\dot{3} \times 0.1\dot{6}$

[5 marks]

Give your answer as a fraction in its simplest form.

$$100x = 53.\dot{3}3333 \dots$$

$$100y = 16.\dot{6}6666 \dots$$

$$10x = 5.\dot{3}3333 \dots$$

$$10y = 1.\dot{6}6666 \dots$$

$$x = 0.5\dot{3}333 \dots$$

$$y = 0.1\dot{6}666 \dots$$

$$90x = 48$$

$$90y = 15$$

$$x = \frac{48}{90}$$

$$x = \frac{24}{45}$$

$$y = \frac{15}{90}$$

$$y = \frac{1}{6}$$

$$\frac{24}{45} \times \frac{1}{6} = \frac{4}{45}$$

$$\frac{4}{45}$$

Answer

Turn over ►





14

Work out $0.\dot{0}8 \div 3.\dot{6}3$

[5 marks]

Give your answer as a fraction in its simplest form.

$$100x = 8.\dot{8}8888 \dots$$

$$100y = 363.\dot{6}36363 \dots$$

$$10x = 0.\dot{8}8888 \dots$$

$$10y = 36.\dot{3}63636 \dots$$

$$x = 0.\dot{0}8888 \dots$$

$$- y = 3.\dot{6}36363 \dots$$

$$90x = 8$$

$$99y = 360$$

$$x = \frac{8}{90}$$

$$y = \frac{360}{99}$$

$$\frac{\cancel{8}^1}{\cancel{90}_{10}} \times \frac{\cancel{99}^{11}}{\cancel{360}_{45}} = \frac{11}{450}$$

$$\frac{11}{450}$$

Answer

15

Work out $\left(0.\dot{2}9\dot{6}\right)^{\frac{2}{3}}$

[5 marks]

Give your answer as a fraction in its simplest form.

$$1000x = 296.\dot{2}96296 \dots$$

$$x = 0.\dot{2}96296 \dots$$

$$999x = 296$$

$$x = \frac{296}{999}$$

$$x = \frac{8}{27}$$

$$x = \frac{2 \times 2 \times 2 \times \cancel{37}}{3 \times 3 \times 3 \times \cancel{37}}$$

$$\left(\frac{8}{27}\right)^{\frac{2}{3}} = \left(\frac{2}{3}\right)^2$$

$$\frac{4}{9}$$

Answer

